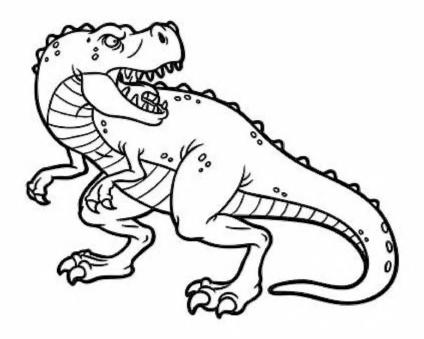
Prep [1] Ceometry-Second Term Unit [3]-Part [1]



Mr. Mahmoud Esmaiel 01006487539=01110882717

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Prep [1] - Second Term - Unit [3] : Geometry And Measurement

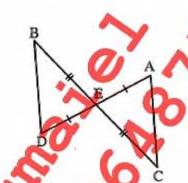
Lesson [1]: Deductive Proof

Example [1]

In the opposite figure:

$$\overline{AD} \cap \overline{BC} = \{E\}$$
 where $AE = DE$ and $BE = CE$

Prove that : \triangle AEC \equiv \triangle DEB



Solutions

Given
$$\overrightarrow{AD} \cap \overrightarrow{BC} = \{E\}$$
 where $\overrightarrow{AE} = \overrightarrow{DE}$, $\overrightarrow{BE} = \overrightarrow{CE}$

R.T.P.
$$\triangle$$
 AEC \equiv \triangle DEB

Proof
$$: \overline{AD} \cap \overline{BC} = \{E\} : m (\triangle AEC) = m (\triangle DEB) (V.O.A)$$

$$\begin{cases}
AE = DE \text{ (given)} \\
CE = BE \text{ (given)} \\
m (\angle AEC) = m (\triangle DEB) \text{ (by proof)}
\end{cases}$$

∴ Δ AEC ≡ Δ DEB

(Q.E.D.)

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قئــوات ذاكــرولى

على تطييق الثليجر ام

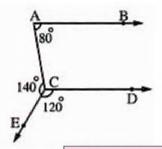
Example [2]

In the opposite figure:

$$m (\angle BAC) = 80^{\circ} m (\angle DCE) = 120^{\circ}$$

and m (∠ ACE) ≥ 140°

Prove that : AB // CD



Solutions

Given
$$m(\angle BAC) = 80^{\circ}$$
, $m(\angle DCE) = 120^{\circ}$,

R.T.P. AB // CD

Proof :
$$m (\angle DCA) + m (\angle DCE) + m (\angle ACE) = 360^{\circ}$$

(accumulative angles at C)

$$\therefore$$
 m (\angle DCA) = 360° - (120° + 140°) = 100°

:.
$$m (\angle BAC) + m (\angle DCA) = 80^{\circ} + 100^{\circ} = 180^{\circ}$$

And they are interior angles in the same side of the transversal AC

: AB // CD

(Q.E.D.)

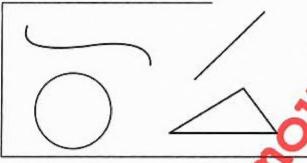
Lesson [2]: Part [1]: The Polygon

Before studying polygons we will study the types of the line as follows.

The simple line

It is the line that does not cut itself.

Examples for the simple line:



The closed line

It is the line that ends where it starts at the same point. It may be simple or non-simple.

Examples for the closed line

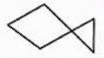






The closed simple line.

The closed simple line.





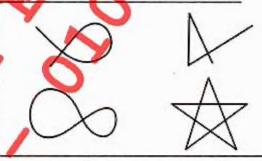
line.

The closed non-simple The closed non-simple

The non-simple line

It is the line that cuts itself once or more.

Examples for the non-simple line:



The open line

It is the line whose starting point is not the end point. It may be simple or non-simple.

Examples for the open line:



The open simple line.



The open simple line.



The open non-simple line.



The open non-simple line.

The Polygon:

It is a simple closed line that consists of three line segments, or more. The polygon is named according to the number of its sides.

Examples for some polygons:



Triangle (3 sides)



Quadrilateral (4 sides)



Pentagon (5 sides)



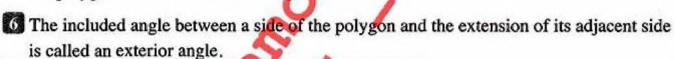
Heptagon (7 sides)

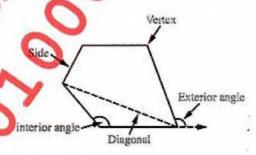


Octagon (8 sides)

Remarks

- Each line segment of the line segments forming the polygon is called a side.
- Each point resulted from intersecting of two adjacent sides of the polygon is called a vertex.
- The sum of the side lengths of the polygon is called the perimeter of the polygon.
- Each line segment joining two non-adjacent vertices of the polygon is called a diagonal of the polygon.
- The included angle between two adjacent sides of the polygon is called an interior angle.





Convex Polygon And Concave Polygon:

In the convex polygon:

If a straight line is drawn to pass through any two consecutive vertices, then the remained vertices lie on one side of this straight line.



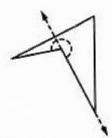


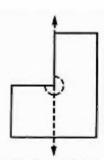
Notice that:

Any interior angle of the convex polygon has measure less than 180°

In the concave polygon:

There are straight lines (one at least) passing through two consecutive vertices and the remained vertices lie on two different sides of the straight line.





Notice that :

There is at least one interior angle of concave polygon of measure more than 180° (reflex angle).

The Sum Of Measures Of The Interior Angles Of The Polygon:

:. The sum of measures of the interior angles of a polygon of n sides equals $(n-2) \times 180^{\circ}$

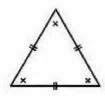
The sum of measures of the exterior angles of a convex polygon of n sides = 360° (taking into account one exterior angle at each vertex)

The Regular Polygon :

The polygon is regular if :

- All its sides are equal in length.
- All its angles are equal in measure.

As examples for the regular polygons:



Equilateral triangle



Square



Regular pentagon



Regular hexagon

The Measure Of The Interior Angle Of A Regular Polygon:

 \therefore The measure of each interior angle of the regular polygon of n-sides = $\frac{(n-2) \times 180^{\circ}}{n}$

For example:

- The measure of each interior angle of the equilateral triangle = $\frac{(3-2) \times 180^{\circ}}{3} = 60^{\circ}$
- The measure of each interior angle of the square = $\frac{(4-2) \times 180^{\circ}}{4} = 90^{\circ}$
- The measure of each interior angle of the regular pentagon = $\frac{(5-2) \times 180^{\circ}}{5} = 108^{\circ}$
- The measure of each interior angle of the regular hexagon = $\frac{(6-2) \times 180^{\circ}}{6} = 120^{\circ}$

Notice that:

The number of the polygon sides = The number of its vertices = The number of its interior angles = The number of its exterior angles

Remarks

The number of sides of the regular polygon in which the measure of one of its interior angles is $x^{\circ} = \frac{360^{\circ}}{180^{\circ} - x}$

Number of diagonals = $n(n-3) \div 2$

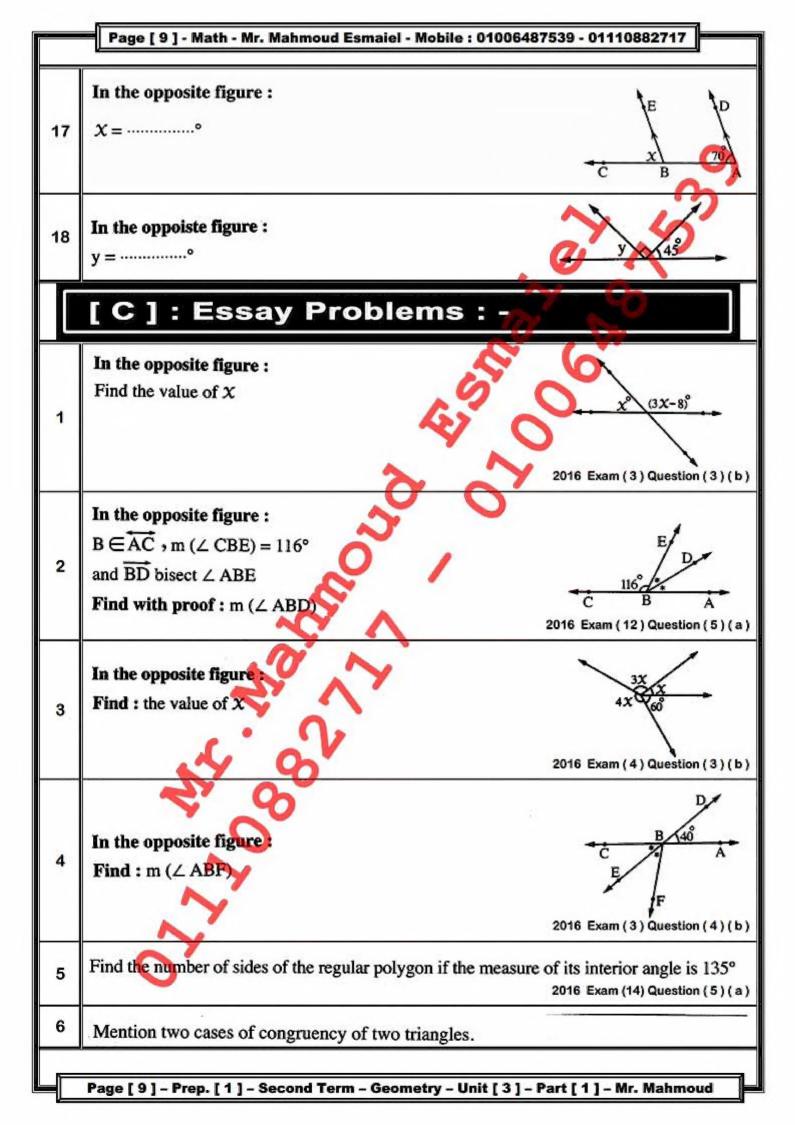
Exercises

[A]: Choose The Correct Answer:

1	The measure of the	e right angle = ···	o				
,	(a) 180	(b) 90	(c) 120	(d) 0	5		
	The angle whose r	measure 90° is	angle.	01 1			
2	(a) acute	(b) right	(c) obtuse	(d) straight			
3	The sum of the me	easures of the acc	cumulative angles at a				
	(a) 90° (b)) 180°	(c) 270°	(d) 360°			
4	If \triangle ABC $\equiv \triangle$ XYZ	Z • then $AB = \cdots$		Y _ W			
4	(a) XY	(b) YZ	(c) XZ 🝌	(d) BC			
5	The angle with me	easure 70° compl	ement angle with meas	sure°			
3	(a) 70	(b) 110	(c) 290	(d) 20			
	The acute angle su	pplements	····· angle.	,			
6	(a) acute	(b) right	(c) obtuse	(d) straight			
	The area of the cir	cle =	0 .				
7	(a) π r	(b) π r ²	(c) 2 π r	(d) $2\pi r^2$			
	The two bisectors	of two adjacent	supplementary angles	included an angle			
8	of measure	°					
	(a) 180	(b) 45	(c) 90	(d) 0			
	The perpendicular to one of two parallel lines is to the other.						
9	(a) parallel	(b) equal	(c) congruent	(d) perpendicular			
10	The edge length of a cube whose total area is 600 cm ² . is cm.						
10	(a) 10	(b) 100	(c) 300	(d) 90			
11	The hexagon has	sides.					
	(a) 5	(b) 6.	(c) 7	(d) 8			
12	The pentagon has	sides.					
100		(b) 4) 6			
13				on of n sides is(d) $\frac{(n-2) \times 180^{\circ}}{n}$			
		$) (n-2) \times 180^{\circ}$	(c) 360°				
	The sum of the me	easures of the in	terior angles of a triang	gle =°			
14	(a) 90	(b) 360	(c) 180	(d) 540			
	2.						

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L	- 1	5	روي	\mathbf{u}	-11-	الللة		ت الد	wing	

1	The angle of measure 180° its type is
2	The measure of the straight angle equals°
3	The measure of the right angle =
4	The sum of the measures of the accumulative angles at a point is
5	The two vertically opposite angles are
6	If two straight lines intersect, then the measures of each two vertically opposite angles are
7	Every two vertically opposite angles are in measure.
8	Each two opposite angles in a parallelogram are
9	If two straight lines intersect, then the sum of measures of any two adjacent angles is
10	If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
11	The opposite figure represents 3 squares each of side length 1 cm. , the perimeter of the figure
12	A circle its radius length 10 cm., then its circumference = (Consider $\pi = 3.14$)
13	The sum of the measures of the exterior angles of the convex polygon =
14	The sum of the measures of the angles of the quadrilateral equals
15	The measure of each interior angle of the regular hexagon is°
16	The measure of each interior angle of the regular pentagon =



		2017 Exam (12) Question (5) (a
7	Using the geometric tools, draw the angle ABC of then bisect it. (don't remove arcs).	of measure 140
8	In the opposite figure : $m (\angle A) = 80^{\circ} \cdot m (\angle D) = 120^{\circ} \cdot m (\angle CBE) = 130^{\circ} \text{ and } B \in \overrightarrow{AE}$ Find with proof : $m (\angle C)$	130 80 A È B A 2016 Exam (6) Question (3) (a
9	In the opposite figure : $F \in \overrightarrow{YZ}$, $m (\angle L) = 70^{\circ}$, $m (\angle Y) = 90^{\circ}$ and $m (\angle LZF) = 120^{\circ}$ Find : $m (\angle X)$	120° X F Z Y 2018 Exam (13) Question (3) (b
10	In the opposite figure : $\overrightarrow{AD} // \overrightarrow{BC}$, \overrightarrow{CF} bisects \angle DCE , m (\angle ABC) = 55°, m (\angle ADC) = 110° Prove that : $\overrightarrow{AB} // \overrightarrow{CF}$	E C B 2017 Exam (11) Question (5) (b
11	In the opposite figure: ABCD is a quadrilateral in which: $m(\angle A) = 90^{\circ}$ Find: the value of X	2018 Exam (11) Question (3) (a
12	In the opposite figure: $\overrightarrow{AB} // \overrightarrow{CD}$, m ($\angle A$) = 50°, $\angle ACE$ is right angle, and m ($\angle E$) = 40° Prove that: $\overrightarrow{AB} // \overrightarrow{EF}$	A B C C F C C F C C F C C C C C C C C C C

Homework

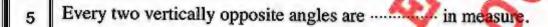
[A]: Choose The Correct Answer:

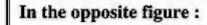
1	The edge length	of a cube whose	e total area is 600 cm	n ² . is cm.	2
1	(a) 10	(b) 100	(c) 300	(d) 90	1 la
2	If the number of angle is (x°) , the (a) 90°	sides of a regula ien X =(b) 108°	ur polygon is 5 and if (c) 120°	the measure of each	interior
3	The perpendicul	ar to one of two (b) equal	parallel lines is (c) congrue	to the other.	ncular
4	(a) 60°	(b) 90°	f the equilateral triang (c) 30°	(d) 120°	1
5	The two bisectors of measure		nt supplementary and	gles included an an	gle
6	The sum of mea (a) 720 °	sures of the exter (b) 120 °	rior angles of the hex (c) 180°	agon =(d) 360 °	
7	The area of the (a) π r	circle = (b) π r ²	(c) 2 π r	(d) 2 π r ²	
8	In all the	following shapes n	$\ln (\angle X) = 60^{\circ} except the $	X Ax	(d)
9	The number of (a) 4	liagonals of a qu (b) 3	adrilateral is (c) 2	 (d) 0	
10	The angle with (a) 70	measure 70° con (b) 110	plement angle with (c) 290	measure ·····° (d) 20	
11	If the measure its sides is		gle of a regular polygo (c) 7	on is 135°, then the n	umber of
	V-7/	\-/	S-7 '	£-7 ~	

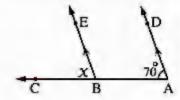
-	Page [12]	- Math - Mr. Mahmou	ıd Esmaiel - Mobile :	01006487539 - 0111088	32717	
12	The St. of	XYZ, then AB = ····		J. Sec.		
	(a) XY	(b) YZ	(c) XZ	(d) BC		
13		gle supplements	····· angle.			
	(a) acute	(b) right	(c) obtuse	(d) straight	~ (
	The area of the	ne shaded part = ······	···· the total area of the	shape.		
14	(a) $\frac{1}{8}$		(b) $\frac{1}{4}$		401	
	(c) $\frac{3}{8}$		(d) $\frac{3}{4}$	0 1		
				*N A		
15	The sum of t	he measures of the in	terior angles of a trian	igle =°		
13	(a) 90	(b) 360	(c) 180	(d) 540		
16	How many sid	des has a regular polygo	n if the measure of each	interior angle of it is 120	7	
10	(a) 5	(b) 6	(c) 7	(d) 8		
17			cumulative angles at a			
	(a) 90°	(b) 180°	(c) 270°	(d) 360°		
18	The sum of t			gon of n sides is		
	(a) $(n-2)$	(b) $(n-2) \times 180^{\circ}$	(c) 360°	$(d) \frac{(n-2) \times 180^{\circ}}{n}$		
40	The measure	of the interior angle	of a regular polygon o	f 18 sides equals ·····		
19	(a) 130°	(b) 140°	(c) 150°/	(d) 160°		
	The angle whose measure 90° is angle.					
20		(b) right	(c) obtuse	(d) straight		
			(C) ootuse	(u) strangin		
21		hassides.	(c) 5 (d) 6		
	(a) 3	(b) 4 of each angle of the r				
22		(b) 180°	(c) 120°	(d) 144°		
	(a) 90°			(u) 144		
23	E1	of the right angle =		(3) 0		
	(a) 180 <	(b) 90	(c) 120	(d) 0		
24			nterior angles of a pe	(d) 540°		
	(a) 360°	(b) 450°	(c) 720°			
25			of a regular pentagon			
197	(a) 900°	(b) 180°	(c) 540°	(d) 108°		
26		has sides.	4.5			
ZŲ	(a) 5	(b) 6	(c) 7	(d) 8		

[B]: Complete the Following:-

- If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
- If two straight lines intersect, then the sum of measures of any two adjacent angles is
- Bach two opposite angles in a parallelogram are
- In the oppoiste figure :







- If two straight lines intersect , then the measures of each two vertically opposite angles are
- 8 The measure of each interior angle of the regular pentagon =
- 9 The two vertically opposite angles are
- 10 The angle of measure 180° its type is
- 11 The measure of each interior angle of the regular hexagon is
- 12 The sum of the measures of the accumulative angles at a point is°
- 13 The sum of the measures of the angles of the quadrilateral equals
- 14 The measure of the right angle =°
- 15 The sum of the measures of the exterior angles of the convex polygon =

	Page [14] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717
16	The measure of the straight angle equals°
17	A circle its radius length 10 cm., then its circumference = (Consider $\pi = 3.14$)
18	The opposite figure represents 3 squares each of side length 1 cm. the perimeter of the figure =
	[C]: Essay Problems:-
1	In the opposite figure : \overline{AD} // \overline{BC} , \overline{CF} bisects \angle DCE , \overline{m} (\angle ABC) = 55° , \overline{m} (\angle ADC) = 110° \overline{E} \overline{CF} Prove that : \overline{AB} // \overline{CF} 2017 Exam (11) Question (5) (b)
2	In the opposite figure : $F \in \overline{YZ}, m (\angle L) = 70^{\circ}$, $m (\angle Y) = 90^{\circ}$ and $m (\angle LZF) = 120^{\circ}$ Find : $m (\angle X)$ $F = Z \qquad Y$ 2018 Exam (13) Question (3) (b)
3	In the opposite figure: $m (\angle A) = 80^{\circ}, m (\angle D) = 120^{\circ},$ $m (\angle CBE) = 130^{\circ} \text{ and } B \in \overline{AE}$ Find with proof $/m (\angle C)$ $2016 \text{ Exam } (6) \text{ Question } (3)(a)$
4	Using the geometric tools, draw the angle ABC of measure 140, then bisect it. (don't remove arcs). 2017 Exam(12) Question(4)(b)
5	In the opposite figure: Find the value of X 2016 Exam (3) Question (3) (b)

6	Find the number of sides of the regular polygon if the mea	asure of its interior angle is 135° 2016 Exam (14) Question (5) (
7	Mention two cases of congruency of two triangles.	2017 Exam (12) Question (5)
8	In the opposite figure : Find : m (∠ ABF)	D B 40° A F 2016 Exam (3) Question (4) (1
9	In the opposite figure : Find : the value of X	3X 4X 60 2016 Exam (4) Question (3) (1
10	In the opposite figure : $B \in \overrightarrow{AC}, m (\angle CBE) = 116^{\circ}$ and \overrightarrow{BD} bisect $\angle ABE$ Find with proof : $m (\angle ABD)$	E D 116° C B A 2016 Exam (12) Question (5) (1
11	In the opposite figure: $\overrightarrow{AB} // \overrightarrow{CD}$, m ($\angle A$) = 50°, $\angle ACE$ is right angle, and m ($\angle E$) = 40° Prove that: $\overrightarrow{AB} // \overrightarrow{EF}$	A B So C C E F
12	In the opposite figure: ABCD is a quadrilateral in which: $m(\angle A) = 90^{\circ}$ Find: the value of X	$D = \frac{3x}{5x}$ 2018 Exam (11) Question (3) (3)

Prep [1] Ceometry-Second Term Unit [3]-Part [2]



Mr. Mahmoud Esmaiel 01006487539-01110882717

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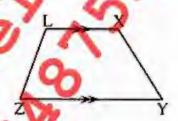
Lesson [2]: Part [2]: The Polygon

Trapezium - Parallelogram - Rectangle - Rhombus - Square

Trapezium:

A quadrilateral in which only two sides are parallel is called a trapezium, as shown in the opposite figure in which:

 $\overline{XL} / \overline{YZ}$



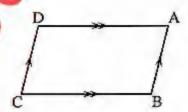
Definition

Parallelogram is a quadrilateral, in which each two opposite sides are parallel.

In the opposite figure

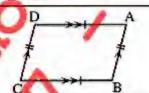
ABCD is a parallelogram because

AB // DC and AD // BC



Properties of parallelogram:

Each two opposite sides are equal in length.



- \bullet AB = DC
- \bullet AD = BC

- Each two opposite angles are equal in measure.
- $m(\angle A) = m(\angle C)$
- $m (\angle B) = m (\angle D)$

- The sum of measures of each two consecutive angles is 180°
- $m (\angle A) + m (\angle B) = 180^{\circ}$
- m (\angle B) + m (\angle C) = 180°
- m (\angle C) + m (\angle D) = 180° • m (\angle D) + m (\angle A) = 180°

- The two diagonals bisect each other.
- AM = CM
- \bullet BM = DM

Remark [1]

The perimeter of the parallelogram = The sum of two consecutive sides $\times 2$

When does a quadrilateral represent a parallelogram ?

A quadrilateral represents a parallelogram if one of the following conditions satisfies

Each two opposite sides are parallel.

Each two opposite sides are equal in length.

Two opposite sides are parallel and equal in length.

Each two opposite angles are equal in measure.

The two diagonals bisect each other.









Rectangle:

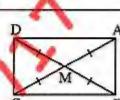
Rectangle is a parallelogram with a right angle.



Properties Of Rectangle:

The rectangle has the same properties of the parallelogram and some additional properties as the following:

The four angles of the rectangle are all equal in measure and the measure of each is 90°



D A

= 90°

AC = BD

and as the two diagonals

 $m (\angle A) = m (\angle B)$

 $= m (\angle C) = m (\angle D)$

2 The two diagonals of the rectangle are equal in length.

bisect each other
then AM = BM = CM = DM

Remark [2]

The perimeter of the rectangle = (length + width) \times 2

Rhombus:

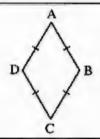
Rhombus is a parallelogram in which two adjacent sides are equal in length.



Properties Of Rhombus:

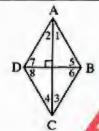
The rhombus has the same properties of the parallelogram and some additional properties as the following :

The four sides of the rhombus are all equal in length.



• AB = BC = CD = DA

The two diagonals of the rhombus are perpendicular and bisect each of its interior angles.



• $\overline{AC} \perp \overline{BD}$ • $m(\angle 1) = m(\triangle 2)$ = $m(\angle 3) = m(\angle 4)$ • $m(\angle 5) = m(\angle 6)$ = $m(\angle 7) = m(\angle 8)$

Remark [3]

The perimeter of the rhombus = the length of one side $\times 4$

Square:

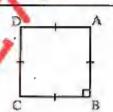
Square is a parallelogram with a right angle and two adjacent sides are equal in length.



Properties Of Square

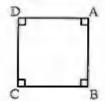
The square has the same properties of the parallelogram and some additional properties as the following:

Its four sides are all equal in length.



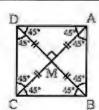
• AB = BC = CD = DA

Its four angles are all equal in measure and each of them is of measure 90°



• m (\angle A) = m (\angle B) = m (\angle C) = m (\angle D) = 90°

Its two diagonals are equal in length, perpendicular and each diagonal bisects the two vertices angles which this diagonal joins.



• AC = BD and hence AM = BM = CM = DM• $\overline{AC} \perp \overline{BD}$

Remark [4]

The perimeter of the square = the length of one side \times 4

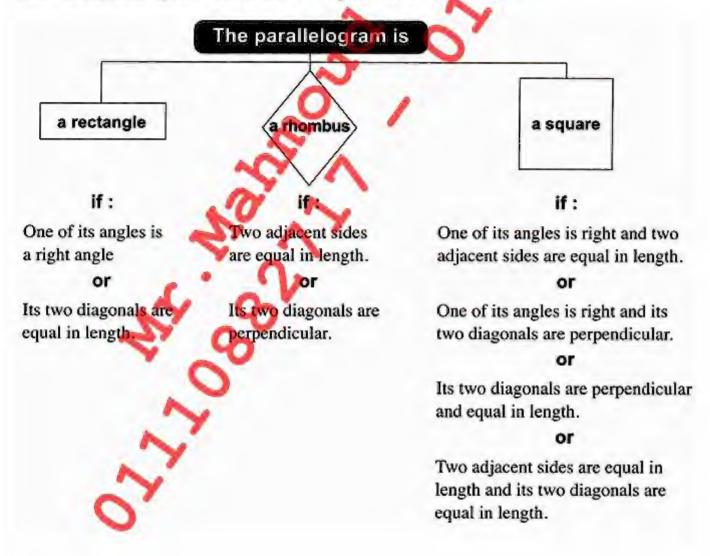
Notice That:-

We can also define the square as follows:

- A square is a rectangle with two adjacent sides equal in length.
- 2 A square is a rectangle with two perpendicular diagonals.
- 3 A square is a rhombus with a right angle.
- A square is a rhombus with two diagnals equal in length.

Notice That: -

To prove that the quadrilateral is a rectangle, a rhombus or a square, we must first prove that it is a parallelogram, as we see in the previous lesson, then:



Toronto.			
Ewa	- 1	00	
Exa	• 11	(F)	

Calculate the sum of the measures of the interior angles of a hexagon.

2014 Exam (12) Question (3)(a)

Find the measure of each interior angle of regular hexagon. 2

2014 Exam (9) Question (4)(a)

How many sides does a regular polygon have if 3 the measure of each interior angle of it is 120°?

2014 Exam (6) Question (3) (b)

Find the number of sides of a regular polygon if the measure of one of its exterior 4 angle is 45°

2015 Exam (5) Question (4) (a)

In the opposite figure:

$$\overrightarrow{EF} \perp \overrightarrow{FB}, \overrightarrow{DA} \cap \overrightarrow{FB} = \{C\},\$$

 $m (\angle ACB) = 66^{\circ} , m (\angle E) = 104^{\circ}$

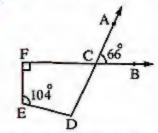
Find: $m(\angle D)$

5

6

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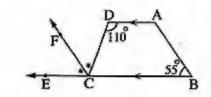


2015 Exam (15) Question (4) (b)

In the opposite figure:

$$m (\angle ABC) = 55^{\circ} m (\angle ADC) = 110^{\circ}$$

Prove that : AB // CF

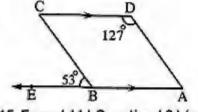


2017 Exam (12) Question (3)(a)

In the opposite figure:

$$\overline{DC}$$
 // \overline{AB} , $\overline{E} \subset \overline{AB}$, \overline{m} ($\angle CBE$) = 53° , \overline{m} ($\angle D$) = 127°

Prove that : AD // BC



2015 Exam (11) Question (3)(a)

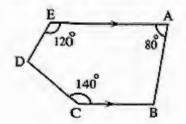
In the opposite figure:

ABCDE is a pentagon in which AE // BC,

$$m (\angle A) = 80^{\circ}$$
, $m (\angle C) = 140^{\circ}$, $m (\angle E) = 120^{\circ}$

Find: (A B)

(2) m (\(\subset D \)



2015 Exam (4) Question (4)(a)

In the opposite figure:

ABCDEF is a hexagon, $m (\angle B) = 90^{\circ}$,

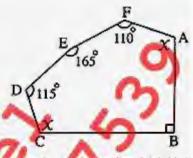
 $m (\angle F) = 110^{\circ}, m (\angle E) = 165^{\circ}, m (\angle D) = 115^{\circ},$

 $m (\angle FAB) = m (\angle DCB) = X$

Find: the value of X

9

10



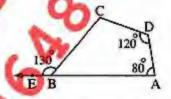
2014 Exam (11) Question (3) (b)

In the opposite figure:

m (\angle A) = 80°, m (\angle D) = 120°

, m (∠ CBE) = 130°

Find: $m (\angle C)$



Model Exam (5) Question (5)(a)

Solutions

1	The sum = $(6-2) \times 180^{\circ} = 720^{\circ}$

- The measure of each interior angle = $\frac{(6-2) \times 180^{\circ}}{6}$
- The number of sides = $\frac{360^{\circ}}{180^{\circ} 120^{\circ}} = 6$ sides
- 4 The number of sides = $\frac{360^6}{45^9}$ = 8 sides

$$\therefore \overrightarrow{DA} \cap \overrightarrow{FB} = \{C\}$$

$$\therefore m (\angle DCF) = m (\angle ACB) = 66^{\circ} \qquad (V.O.A.)$$

5 From quadrilateral CDEF

$$\therefore$$
 m (\angle D) = 360° - (104° + 66° + 90°) = 100° (The req.)

: AD // BC , DC is a transversal

(alternate angles)

, ∵ CF bisects ∠ DCE

:. m (
$$\angle$$
 FCE) = $\frac{110^{\circ}}{2}$ = 55°

$$\rightarrow m (\angle B) = m (\angle FCE) = 55^{\circ}$$

and they are corresponding angles.

:. AB // CF

6

(Q.E.D.)

$$\therefore$$
 m (\angle A) + m (\angle D) = 180°

(Two interior angles in the same side of the transversal).

$$m (\angle A) = 180^{\circ} - 127^{\circ} = 53^{\circ}$$

$$\therefore m (\angle A) = m (\angle CBE) = 53^{\circ}$$

and they are corresponding angles.

$$\therefore m (\angle A) + m (\angle B) = 180^{\circ}$$

Two interior angles in the same side of

the transversal.

∴ m (∠ B) =
$$180^{\circ} - 80^{\circ} = 100^{\circ}$$
 (First req.)

From pantagon ABCDE:

$$\therefore m (\angle D) = 540^{\circ} - (120^{\circ} + 80^{\circ} + 100^{\circ} + 140^{\circ})$$

= 100° (Second req.)

$$\therefore 2 \times = 720^{\circ} - (110^{\circ} + 90^{\circ} + 165^{\circ} + 115^{\circ}) = 240^{\circ}$$

$$\therefore X = 240^{\circ} \div 2 = 120^{\circ}$$
 (The req.)

$$\therefore$$
 m (\angle ABC) = 180° - 130° = 50°

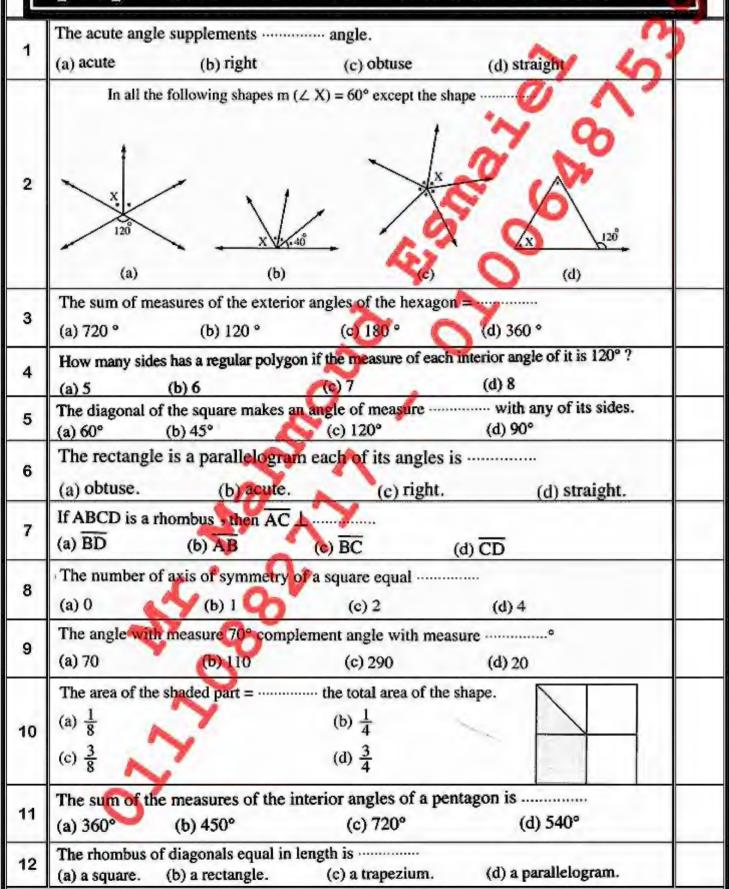
10 : From the quadrilateral ABCD :

$$m (\angle C) = 360^{\circ} - (50^{\circ} + 80^{\circ} + 120^{\circ})$$

$$=360^{\circ}-250^{\circ}=110^{\circ}$$
 (The req.)

Exercises

[A]: Choose The Correct Answer:



	Page [9] -	Math - Mr. Mahmoud	Esmaiel - Mobile : (01006487539 - 01110882717	
40	The measure of	of the interior angle of	a regular polygon o	f 18 sides equals ·····	
13	(a) 130°	(b) 140°	(c) 150°	(d) 160°	
14	The diagonals	are equal in length an	d perpendicular in ··		
	(a) square.	(b) rhombus.	(c) rectangle.	(d) parallelogram.	Y)
15	The measure of	of the right angle = ····	6	A	
	(a) 180	(b) 90	(c) 120	(d) 0	
		parallelogram in whic	ch BC = 8 cm. and C	CD = 6 cm then its	
16	perimeter = ···		(-) 40	(d) 56 cm.	
	(a) 14 cm.	(b) 28 cm.	(c) 48 cm.	111	
17		th of the rhombus whi	-		
	(a) 6	(b) 9	(c) 18	(d) 4	
18		square, then $(AC)^2 =$	4.3.3	~	
	(a) AB	(b) (AB) ²	(c) 2 (AB) ²	(d) 4 (AB) ²	
19	If \triangle ABC $\equiv \triangle$	XYZ , then AB =		7	
	(a) XY	(b) YZ	(c) XZ	(d) BC	
20		th of a cube whose to			
	(a) 10 The sum of th	(b) 100 e measures of the inte	(c) 300	(d) 90	-
21			7		
	(a) 90	(b) 360	(c) 180	(d) 540	
22		of each angle of the re			
	(a) 90°	(b) 180°	(c) 120°	(d) 144°	
23	(a) square	·· the two diagonals are (b) rhombus		not equal in length. (d) parallelogram	
		rallelogram , m (∠ A)			
24	(a) 110	(b) 35	(c) 70	(d) 140	
	In a parallelogr	am if the adjacent sides a	are equal in the length	then the shape is	
25	(a) square.	(b) rhombus.	(c) rectangle.	(d) trapezium.	
	ABCD is a squ	are , then m (∠ BAC)	=°		
26	(a) 90	(b) 60	(c) 45	(d) 30	
	If the side leng	throf a square is 10.5 cm	n , then the perimeter	r of this square = cm.	
27	(a) 40	(b) 42		(d) 100	
			1.6	length and perpendicular is	
28	called				
	(a) rectangle.	(b) square.	(c) rhombus.	(d) trapezium.	

[B]: Complete the Following: -

1	The angle of measure 180° its type is
2	If two straight lines intersect, then the measures of each two vertically opposite angles are
3	A circle its radius length 10 cm., then its circumference =
4	Each two opposite angles in a parallelogram are
5	If ABCD is a parallelogram in which: m (∠ A) = 120°, then m (∠ B) =°
6	The rectangle is a parallelogram in which one of it's angles is
7	The number of axis of symmetry of square is
8	The two vertically opposite angles are
9	The opposite figure represents 3 squares each of side length 1 cm. , the perimeter of the figure =
10	If two opposite sides in the quadrilateral are parallel, then it is called
11	ABCD is parallelogram in which $m (\angle A) = 100^{\circ}$, then $m (\angle D) = \dots$
12	If ABCD is rectangle and if AB = 4 cm., BD = 5 cm., then the area of the rectangle =
13	Square is a rectangle in which
14	The sum of the measures of the accumulative angles at a point is°
15	If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
16	The measure of each interior angle of the regular pentagon =

	Page [11] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717		
17	If ABCD is a parallelogram in which m (\angle A) = 80°, then m (\angle B) =		
18	Two diagonals are equal in length and not perpendicular in		
19	The rhombus with a right angle is		
20	The measure of the right angle =°		
21	If two straight lines intersect, then the sum of measures of any two adjacent angles is		
22	The measure of each interior angle of the regular hexagon is		
23	ABCD is a parallelogram in which m ($\angle A$) = 60° , then m ($\angle B$) =		
24	In the parallelogram XYZL, if m ($\angle X$) = $\frac{1}{2}$ m ($\angle Y$), then m ($\angle Y$) =°		
25	The length of the side of a rhombus whose perimeter is 24 cm. equals cm.		
26	In the oppoiste figure : y =		
27	The measure of the straight angle equals°		
28	Each two opposite angles in a parallelogram are		
29	The sum of the measures of the angles of the quadrilateral equals		
30	ABCD is a parallelogram in which m (\angle A) = 50°, then m (\angle B) =		
31	In the parallelogram XYZL, if $m (\angle X) = \frac{1}{3} m (\angle Y)$, then $m (\angle L) = \dots$		
32	The number of axes of symmetry of the rhombus is axes.		
33	In the opposite figure : $x + y = \dots$		

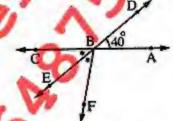
[C]: Essay Problems: -

Using the geometric tools, draw the angle ABC of measure 140, then bisect it. (don't remove arcs).

2017 Exam (12) Question (4) (b)

In the opposite figure :

Find: m (∠ ABF)



2016 Exam (3) Question (4) (b)

In the opposite figure:

3

4

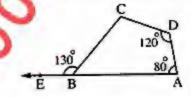
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6

 $m (\angle A) = 80^{\circ}, m (\angle D) = 120^{\circ},$

 $m (\angle CBE) = 130^{\circ} \text{ and } B \in \overline{AE}$

Find with proof: $m(\angle C)$



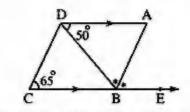
2016 Exam (6) Question (3)(a)

In the opposite figure:

DA // BE , BA bisects ∠ DBE

 $m (\angle ADB) = 50^{\circ} \text{ and } m (\angle C) = 65^{\circ}$

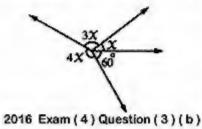
Prove that : ABCD is a parallelogram.



2016 Exam (13) Question (4) (a)

In the opposite figure :

Find: the value of X

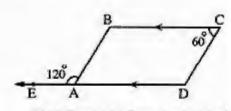


In the opposite figure

 $E \in \overrightarrow{DA}$, $m (\angle EAB) = 120^{\circ}$

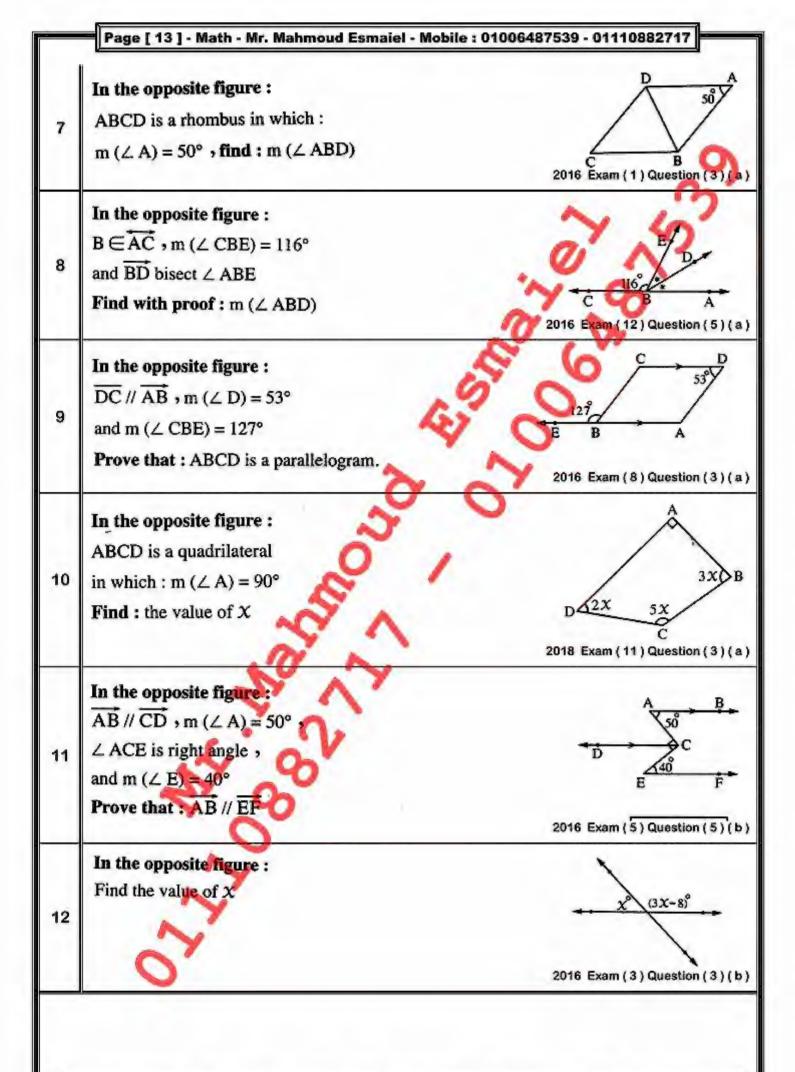
 $, m (\angle C) = 60^{\circ} , \overrightarrow{DA} // \overrightarrow{CB}$

Prove that : ABCD is a parallelogram



2018 Exam (4) Question (5) (a)





Homework

[A]: Choose The Correct Answer:

1	The side length	of the rhombus w	hich its perimeter 3	6 cm. is c	m.	
	(a) 6	(b) 9	(c) 18	(d) 4	.40	
2	ABCD is a para	llelogram → m (∠ /	A) = 70° , then m (2	(C) =	1	
	(a) 110	(b) 35	(c) 70	(d) 140	0	
3	The two diagon	ials are equal in le	ngth and not perper	idicular in		
3	(a) a rectangle	(b) a square	(c) a rhombus	(d) a parallelog	ram	
	If the number of	sides of a regular	polygon is 5 and if	he measure of each	interior	
4	(a) 90°	nen $x = \dots$ (b) 108°	(a) 1200			
		, ,	(c) 120° cof a regular polygor	(d) 180° n is 135°, then the nu	mber of	
5	its sides is		^	~		
	(a) 6	(b) 4	(c) 7	(d) 8		
6			are perpendicular an		1.	
	(a) square	(b) rhombus	(c) rectangle	(d) parallelogram		
7			of a regular pentage			
	(a) 900°	(b) 180°	(c) 540°	(d) 108°		
8	(a) 3	(b) 4. (b)	(c) 5	(d) 6		
•		ne exterior angle of	the equilateral triangle) =		
9	(a) 60°	(b) 90°	(c) 30°	(d) 120°	1	
40	The measure of	each angle of the	egular hexagon is			
10	(a) 90°	(b) 180°	(c) 120°	(d) 144°		
	The sum of the	measures of the ex	terior angles of a pol	lygon of n sides is	1000	
11	(a) (n - 2)	(b) $(n-2) \times 180^{\circ}$	(c) 360°	(d) $\frac{(n-2)\times}{n}$	180-	
	The two bisecto	ors of two adjacent	t supplementary ang	les included an ang	le	
12	of measure					
	(a) 180	(b) 45	(c) 90	(d) 0		
13	The hexagon ha	s ·····sides.				
10	(a) 5	(b) 6	(c) 7	(d) 8		
14	The sum of the measures of the interior angles of a triangle =°					
, -	(a) 90	(b) 360	(c) 180	(d) 540		

	Page [15] - I	vatn - Mr. Manmoud	Esmaiel - Mobile : U	1006487539 - 01110882717	
15	The perpendicular to one of two parallel lines is to the other.				
15	(a) parallel	(b) equal	(c) congruent	(d) perpendicular	
16	The angle whose measure 90° is angle.				
	(a) acute	(b) right	(c) obtuse	(d) straight	
	The area of the circle =				
17	(a) π r	(b) πr^2	(c) 2 π r	(d) 2 π r	
18	The edge length	of a cube whose tota	al area is 600 cm ² . is	cm.	
10	(a) 10	(b) 100	(c) 300	(d) 90	
19		measures of the accu (b) 180°	mulative angles at a p (c) 270°	point = (d) 360°	
00		are of side length 3 cr	m is cm ²	7 20	
20	(a) 9	(b) 6	(c) 12	(d) 3	
21	The perimeter of	of a square with side	length 6 cm.	cm.	
21	(a) 30	(b) 36	(c) 24	(d) 216	
	The diagonal of	square divided its ve	rtex angle in two ang	les of the measure of each of	
22	them is		5		
	(a) 30°	(b) 45°	(c) 60°	(d) 90°	
23	If $\triangle ABC \equiv \triangle X$	YZ , then AB =	4		
	(a) XY	(b) YZ	(c) XZ	(d) BC	
24	If the side length of a square is 10.5 cm., then the perimeter of this square = cm.				
-	(a) 40 (b) 42 (c) 50 (d) 100				
	* The parallelo		gonals are equal in le	ngth and perpendicular is	
25			(-) shambus	(A) transmisses	
	(a) rectangle.	(b) square.	(c) rhombus.	(d) trapezium.	
26		f perpendicular diago		(4)	
		am. (b) a square.		7 V 10	
27	If ABCD is a rh (a) 148°	ombus and m (∠ AC (b) 161°			
	` '	A .	(c) 116°	(d) 32°	
28		uare then $(AC)^2 = $			
	(a) AB	y (b) (AB) ²	(c) $2 (AB)^2$	$(d) 4 (AB)^2$	
00	ABCD is a square → then m (∠ BAC) = ······°				
29	(a) 90	(b) 60	(c) 45	(d) 30	
20	If ABCD is a parallelogram, then $m (\angle A) = m (\angle \cdots)$				
30	(a) B	(b) C	(c) D (e	d) nothing	

[B]: Complete the Following: -

- 1 The angle of measure 180° its type is
- 2 The two vertically opposite angles are

- 5 The number of axes of symmetry of the rhombus is axes
- If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
- 8 ABCD is a parallelogram in which $m(\angle A) = 60^{\circ}$, then $m(\angle B) = \cdots$
- In the parallelogram XYZL, if $m(X) = \frac{1}{3}m(\angle Y)$, then $m(\angle L) = \dots$
- 10 In the opposite figure :



- ABCD is a parallelogram in which m ($\angle A$) = 50°, then m ($\angle B$) =
- 15 The two diagonals of the rhombus are
- 16 If ABCD is a parallelogram in which: $m (\angle A) = 120^{\circ}$, then $m (\angle B) = \dots$
- 17 Square is a rectangle in which

	Page [17] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717		
18	If two straight lines intersect, then the sum of measures of any two adjacent angles is		
19	The sum of the measures of the angles of the quadrilateral equals		
20	ABCD is a parallelogram in which m (∠ A) = 130°, then m (∠ B) = ······°		
21	Each two opposite angles in a parallelogram are		
22	If ABCD is rectangle and if AB = 4 cm BD = 5 cm. 5 then the area of the rectangle =		
23	The measure of the right angle =		
24	Each two opposite angles in a parallelogram are		
25	The parallelogram whose diagonals are equal in length and not perpendicular is		
26	A circle its radius length 10 cm., then its circumference = (Consider $\pi = 3.14$)		
27	ABCD is parallelogram in which m (\angle A) = 100°, then m (\angle D) =		
28	The rhombus with a right angle is		
29	The measure of the straight angle equals		
30	The sum of the measures of the exterior angles of the convex polygon =		
31	If two straight lines intersect, then the measures of each two vertically opposite angles are		
32	If two opposite sides in the quadrilateral are parallel, then it is called		
33	Two diagonals are equal in length and not perpendicular in		
34	In the oppoiste figure : $y = \dots$		

C]: Essay Problems: -

In the opposite figure:

 $\overline{DC} // \overline{AB}$, m ($\angle D$) = 53°

and m (∠ CBE) = 127°

1

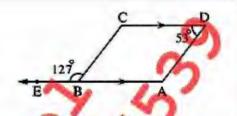
2

3

4

7

Prove that : ABCD is a parallelogram.



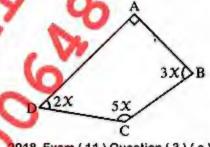
6 Exam (8) Question (3)(a)

In the opposite figure:

ABCD is a quadrilateral

in which: $m(\angle A) = 90^{\circ}$

Find: the value of X



018 Exam (11) Question (3)(a)

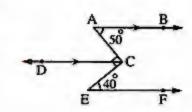
In the opposite figure:

 $\overrightarrow{AB} / (\overrightarrow{CD}), m (\angle A) = 50^{\circ},$

∠ ACE is right angle,

and m (\angle E) = 40°

Prove that : AB // EF



2016 Exam (5) Question (5) (b)

In the opposite figure:

Find the value of X



2016 Exam (3) Question (3) (b)

- Find the number of sides of the regular polygon if the measure of its interior angle is 135° 5 2016 Exam (14) Question (5)(a)
- Mention two cases of congruency of two triangles. 6

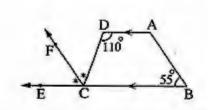
2017 Exam (12) Question (5) (a)

In the opposite figure:

AD // BC, CF bisects ∠ DCE

 $m (\angle ABC) = 55^{\circ} , m (\angle ADC) = 110^{\circ}$

Prove that : AB // CF



		2017 Exam (11) Question (5) (1
8	In the opposite figure : ABCD is a square $\cdot E \subseteq \overrightarrow{BC} \cdot \overrightarrow{AC} /\!\!/ \overrightarrow{DE}$ Prove that : ACED is a parallelogram.	D / E C E Model 2018 Exam (1) Question (5) (1)
9	In the opposite figure : $F \in \overrightarrow{YZ}$, $m (\angle L) = 70^{\circ}$, $m (\angle Y) = 90^{\circ}$ and $m (\angle LZF) = 120^{\circ}$ Find: $m (\angle X)$	F Z Y 2018 Exam (13) Question (3) (1
10	In the opposite figure: ABCD is a square , find in degrees the value of each of X and y	D X X X 102 E Y Y E P E 2018 Exam (12) Question (4) (2)
11	In the opposite figure: ABCD is a parallelogram in which: m(\(\alpha \) B) = 115°, AB = 8 cm. and AD = 5 cm. Find with proof: (1) m(\(\alpha \) D) (2) The perimeter of parallelogram ABCD	2016 Exam (14) Question (4) (
12	In the opposite figure: $E \in \overline{BC}$, $m(\angle BAE) = 45^{\circ}$, $m(\angle AEB) = 70^{\circ}$, $m(\angle D) = 65^{\circ}$ and $m(\angle C) = 115^{\circ}$ Prove that: ABCD is a parallelogram.	D A 45 45 70 E

Prep [1] Ceometry-Second Term Unit [3]-Part [3]



Mr. Mahmoud Esmaiel 01006487539-01110882717

الاســـم

Lesson [3]: The Triangle

Theorem (1)

The sum of the measures of the interior angles of a triangle is 180°

Given

ABC is a triangle

R.T.P.

$$m (\angle A) + m (\angle B) + m (\angle ACB) = 180^{\circ}$$

Construction

Draw CX // AB

Proof

∴ ∠ XCY is a straight angle

$$\therefore$$
 m (\angle XCA) = m (\angle A) (alternate angles

, m (
$$\angle$$
 YCB) = m (\angle B) (alternate angles)

$$m (\angle A) + m (\angle ACB) + m (\angle B) = 180^{\circ}$$

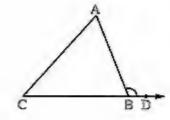
(Q.E.D.)

The exterior angle of the triangle

In the opposite figure:

If ABC is a triangle, D ∈ CB and D ∉ CB, then ∠ ABD is called an exterior angle of A ABC

$$\therefore m (\angle ABD) = m (\angle A) + m (\angle C)$$

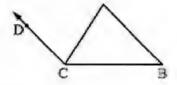


Notice That:

In the opposite figure :

∠ ACD is not an exterior angle of △ ABC

because D∉BC



The measure of the exterior angle of a triangle :

The measure of the exterior angle of a triangle is equal to the sum of the measures of its non adjacent interior angles.

The measure of the exterior angle of a triangle is greater than the measure of any interior angle of the triangle except its adjacent angle.

Remark [1]

If two angles of one triangle equal two angles of another triangle in measure, then the third angle of the first triangle is equal in measure to the third angle of the other triangle.

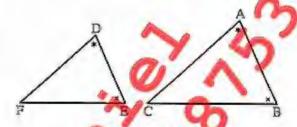
In AA ABC and DEF,

if $m (\angle A) = m (\angle D)$ and $m (\angle B) = m (\angle E)$,

then $m (\angle C) = m (\angle F)$

"You can check the truth of the previous

by measuring"



Remark [2]

- If the sum of measures of two angles in a triangle equals 90°, then the third angle is right.
- If the sum of measures of two angles in a triangle is less than 90°, then the third angle is obtuse.
- If the sum of measures of two angles in a triangle is more than 90°, then the third angle is acute.

Remark [3]

If the measure of an angle in a triangle equals the sum of measures of the other two angles, then the triangle is right-angled.

Theorem (2)

The ray drawn from the midpoint of a side of a triangle parallel to another side bisects the third side.

Given

D is the midpoint of AB, DE // BC

R.T.P.

E is the midpoint of AC

Construction

Draw AX // BC

Proof

: AX // DE // BC

, AB and AC are two transversals

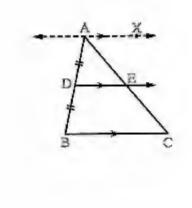
to them at D and E respectively.

$$AD = DB$$

$$\therefore AE = EC$$

.. E is the midpoint of AC

(Q.E.D.)



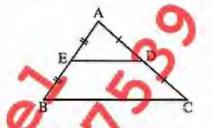
Corollary

The line segment joining the midpoints of two sides of a triangle is parallel to the third side.

In the opposite figure:

If ABC is a triangle in which D is the midpoint of \overline{AC} ,

E is the midpoint of \overline{AB} , then : $\overline{ED} // \overline{BC}$



Theorem (3)

The length of the line segment joining the midpoints of two sides of a triangle is equal to half the length of the third side.

Given

ABC is a triangle, D is the midpoint of \overline{AB} , H is the midpoint of \overline{AC}

R.T.P.

$$DH = \frac{1}{2}BC$$

Construction

Draw HO // AB to cut BC at O



: D is the midpoint of AB, H is the midpoint of AC

.: DH // BC (corollary)

, .: HO // AB (construction) , H is the midpoint of AC

.. O is the midpoint of BC

$$\therefore$$
 BO = $\frac{1}{2}$ BC

. The figure DHOB is a parallelogram.

 $\therefore DH = BO = \frac{1}{2}BC$

(Q.E.D.)

Examples:

In the opposite figure:

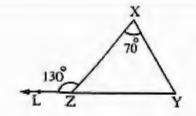
XYZ is a triangle $(\angle XZL) = 130^{\circ}$, m ($\angle XZL$) = 130°,

 $m(\angle X) = 70^{\circ}$

1

2

Find with proof: (1) m (\angle Y) (2) m (\angle YZX)

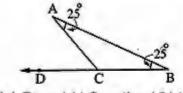


2015 Exam (9) Question (5) (a)

In the opposite figure:

 $m (\angle A) = m (\angle B) = 25^{\circ}$

Find: m (∠ ACD)



Model Exam (1) Question (3)(a)

	Page [5] - Math - Mr. Mahmoud Esmaiel - Mobile : 010	006487539 - 01110882717
3	In the oposite figure: $\overline{DE} // \overline{BC}, m (\angle DAB) = 82^{\circ}$ and $m (\angle D) = 32^{\circ}$ Find by proof: $m (\angle B)$	D E 32A 82 32A 2016 Exam (7) Question (3) (a)
4	In the opposite figure : \overrightarrow{DE} // \overrightarrow{OH} // \overrightarrow{BC} , m (\angle ADE) = 120°, m (\angle AOH) = 135° Find the measures of the angles of : \triangle ABC	H O D E 135° A 120° B 2014 Exam (2) Question (3) (a)
5	In the opposite figure : EDCF is a quadrilateral Δ ABC is an equilateral triangle where $\overline{DB} \cap \overline{AF} = \{C\}$ Find with proof : m (\angle F)	2015 Exam (5) Question (4) (b)
6	In the opposite figure : \overline{AB} and \overline{ED} are perpendicular to \overline{BD} , $\overline{BD} \cap \overline{AO} = \{C\}$; $m (\angle A) = 30^{\circ}$, $m (\angle EOC) = 120^{\circ}$. Find : $m (\angle E)$	D C B 120 B E O Model Exam (2) Question (4) (b)
7	In the opposite figure: ABC is triangle in which D, E and F are the midpoints of AB, BC and CA respectively, BC = 16 cm., AC = 12 cm. Find the perimeter of the quadrilateral: DECF wi	C E B
	0	

In the opposite figure:

8

9

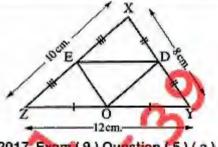
10

11

D , O and E are midpoints of \overline{XY} , \overline{YZ} and \overline{XZ} respectively.

XY = 8 cm. YZ = 12 cm. XZ = 10 cm.

Find with proof: The perimeter of \triangle EOD



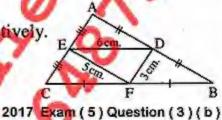
2017 Exam (9) Question (5) (a)

In the opposite figure:

E, D and F are the midpoints of AC, AB and BC respectively.

ED = 6 cm., DF = 3 cm. and EF = 5 cm.

Find with proof: The perimeter of \triangle ABC

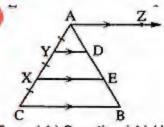


In the opposite figure:

AZ // YD // XE // CB,

AY = YX = XC, AB = 18 cm.,

Find: The length of EB



Model Exam (1) Question (4) (b)

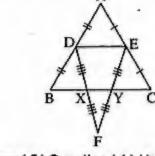
In the opposite figure:

D is the midpoint of AB, E is the midpoint of AC

 $DX = XF \cdot EY = FY$

, BC = 12 cm.

Find: The length of



2017 Exam (5) Question (4) (b)

Solutions

- ∵ ∠ XZL is an exterior angle of Δ XYZ
- \therefore m (\angle Y) = 130° 70° = 60°
- ∴ From ∆ XYZ : m (∠YZX) = 180° (70° + 60°)

= 50° (Second reg.)

- $m(\angle A) = m(\angle B) = 25^{\circ}$
- → ∠ ACD is an exterior angle of △ ABC
 - $m (\angle ACD) = 25^{\circ} + 25^{\circ} = 50^{\circ}$ (The req.)

(The req.)

(The req.)

(The req.)

(The req.)

(The req.)

			\therefore The perimeter of DECF = $6 + 8 + 6 + 8$
3	∴ \overrightarrow{DE} // \overrightarrow{BC} → \overrightarrow{CD} is a transversal ∴ m (\angle C) = m (\angle D) = 32° (alternate angles) → ∴ \angle DAB is an exterior angle of \triangle ABC ∴ m (\angle B) = 82° – 32° = 50° (The req.)		= 28 cm. (The In \triangle XYZ: \because E is the midpoint of \overline{XZ} \Rightarrow O is the midpoint of \overline{ZY} \therefore EO = $\frac{1}{2}$ XY = $\frac{1}{2}$ × 8 = 4 cm.
4	∴ \overrightarrow{OH} // \overrightarrow{BC} → \overrightarrow{OB} is a transversal ∴ m (\angle B) + m (\angle O) = 180° (Two interior angles in the same side of the transversal) ∴ m (\angle B) = 180° - 135° = 45° ∴ \overrightarrow{DE} // \overrightarrow{BC} → \overrightarrow{CD} is a transversal ∴ m (\angle C) + m (\angle D) = 180°	8	
	(Two interior angles in the same side of the transversal) $\therefore m (\angle C) = 180^{\circ} - 120^{\circ} = 60^{\circ}$ In \triangle ABC: $\therefore m (\angle BAC) = 180^{\circ} - (45^{\circ} + 60^{\circ}) = 75^{\circ}$ (The req.)	4	 ∴ In △ABC: ∴ D is the midpoint of AB ∴ E is the midpoint of AC ∴ BC = 2 DE = 2 × 6 = 12 cm. ∴ D is the midpoint of AB
5	∴ \triangle ABC is an equilateral triangle. ∴ $m (\angle ACB) = \frac{180^{\circ}}{3} = 60^{\circ}$ ∴ $m (\angle DCF) = m (\angle ACB) = 60^{\circ}$ (V.O.A) From quadrilateral EDCF: ∴ $m (\angle F) = 360^{\circ} - (60^{\circ} + 120^{\circ} + 118^{\circ})$ $= 62^{\circ}$ (The req.)	9	 F is the midpoint of BC ∴ AC = 2 DF = 2 × 3 = 6 cm. ∵ E is the midpoint of AC F is the midpoint of BC ∴ AB = 2 EF = 2 × 5 = 10 cm. ∴ the perimeter of Δ ABC = 12 + 6 + 10 = 28 cm. (The
6	In △ ABC: m (∠ ACB) = 180° – $(90^{\circ} + 30^{\circ}) = 60^{\circ}$, $\overline{BD} \cap \overline{AO} = \{C\}$ ∴ m (∠ ACB) = m (∠ OCD) = 60° (V.O.A) ∴ m (∠ E) = 360° – $(60^{\circ} + 120^{\circ} + 90^{\circ}) = 90^{\circ}$	10	$\therefore \overrightarrow{AZ} / \overrightarrow{YD} / \overrightarrow{XE} / \overrightarrow{CB} \cdot AY = YX = XC$ $\therefore AD = DE = EB$ $\therefore EB = \frac{18}{3} = 6 \text{ cm.}$ (The
7	∴ D is the midpoint of \overline{AB} ⇒ E is the midpoint of \overline{BC} ∴ DE = $\frac{1}{2}$ AC = $\frac{1}{2}$ × 12 = 6 cm. ⇒ ∴ D is the midpoint of \overline{AB} ⇒ F is the midpoint of \overline{AC} ∴ DF = $\frac{1}{2}$ BC = $\frac{1}{2}$ × 16 = 8 cm.	11	In \triangle ABC: \therefore D is the midpoint of \overline{AB} , E is the midpoint of \overline{AC} . \therefore DE = $\frac{1}{2}$ BC = $\frac{1}{2}$ × 12 = 6 cm. • In \triangle EFD: \therefore X is the midpoint of \overline{FD} . \therefore Y is the midpoint of \overline{EF} . \therefore XY = $\frac{1}{2}$ ED = $\frac{1}{2}$ × 6 = 3 cm. (The
	$∴ CE = \frac{1}{2} BC = \frac{1}{2} \times 16 = 8 \text{ cm.}$ $∴ CF = \frac{1}{2} AC = \frac{1}{2} \times 12 = 6 \text{ cm.}$		

Exercises

[A]: Choose The Correct Answer:

1	The sum of mea (a) 90°	sures of the angles (b) 180°	of a triangle is (c) 270°	(d) 360°	5
2	The parallelogra		onals areis	called a rectangle.	other
3	The rectangle i	s a parallelogran (b) acute.	each of its angles (c) right,	~ VI	ght.
4	The two diagona (a) a rectangle	als are equal in len (b) a square	gth and not perpend (c) a rhombus	icular in(d) a parallelogram	
5	The sum of meas (a) 720°	sures of the exterior (b) 120°	angles of the hexago (c) 180 °	on =	
6	The area of the α (a) π r	ircle = (b) π r ²	(c) 2πr	(d) 2 π r ²	
7		igure: points of AB and A then BC =	4	X 10 cm	a. Y
8		line segment joining the length of the lengt		wo sides of a triangle (d) third	
9	Any triangle has (a) reflex	at least two (b) obtuse	angles.	(d) right	
10	The diagonals ar	e equal in length at (b) rhombus.	nd perpendicular in (c) rectangle.	(d) parallelograr	n.
11	In thet (a) square	he two diagonals a (b) rhombus	re perpendicular and (c) rectangle	not equal in length. (d) parallelogram	
12	The measure of the	e exterior angle of th (b) 90°	e equilateral triangle =	(d) 120°	:

				: 01006487539 - 0111	0882717
	The two bised	ctors of two adjace	nt supplementary an	gles included an angle	
13	of measure ···	0			
	(a) 180	(b) 45	(c) 90	(d) 0	
	In the opposi	ite figure :			À
	X, Y are mid	points of AB, AC	respectively , BC =	10 cm.	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
14	, then XY =	cm.		×/	-X-1
	(a) 5		(b) 20	0 /	
	(c) 10		(d) 30	***	
	The length of	the line segment jo	ining between two m	idpoints of two sides of	C C
15	a triangle = ····	length of its	s third side.	S CV	
	(a) $\frac{1}{5}$	(b) $\frac{1}{4}$	(c) $\frac{1}{3}$	(d) 1	
	The sum of th	e interior angles of	f an isosceles triangle	<u> </u>	
16	(a) 180°	(b) 90°	(c) 60°	(d) 45°	
	If ARCD is a	square , then (AC)	12_	~	
17	(a) AB	(b) (AB) ²	(c) 2 (AB) ²	(d) 4 (AB) ²	
		are, then m (∠ BA	<u> </u>	(d) 4 (AB)	
18	(a) 90	(b) 60	(c) 45	(4) 20	
				(d) 30	
19			le of a regular pentag		
	(a) 900° If the number	(b) 180°		(d) 108° the measure of each in	11
20	angle is (X°) ,	then $X = \cdots$	a polygon is a gift if	the measure of each in	terior
	(a) 90°	(b) 108°	(c) 120°	(d) 180°	
21	The perpendic	cular to one of two	parallel lines is	····· to the other.	
	(a) parallel	(b) equal	(c) congrue	nt (d) perpendicu	llar
	In the opposi	te figure :		A	
22	ED : BC =	0	2000	E	D
	(a) 1 : 1	~	(b) 1 : 2	1	
	(c) 1:3	that the ship with	(d) 1 : 4	C triangle is th	B
23	side.	em joining the midj	points of two sides of	a triangle is th	. ama
		ular to (b) equal to	(c) parallel t	o (d) bisect to	
			exterior angles of tr		
24	(a) 90°	(b) 180°	(c) 360°	(d) 120)°
	11.				

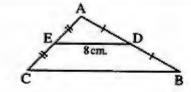
[B]: Complete the Following:-

- 1 Any triangle has at least two interior angles.
- 2 The number of axis of symmetry of the isosceles triangle =
- The sum of the measures of the interior angles of a triangle
- 4 The measure of the exterior angle of a triangle is
- The measure of the exterior angle of any vertex of the equilateral triangle =
- The measure of the exterior angle of a triangle is equal to the sum of
- The ray drawn from the midpoint of a side of a triangle parallel to another side the third side.
- The ray drawn parallel to one side of triangle and passing through the midpoint of another side
- 9 The line segment joining midpoints of two sides of a triangle is
- The line segment joining between two midpoints of two sides of triangle is parallel to
- The line segment joining the midpoint of two sides of a triangle is
 the third side.
- The length of the line segment joining the midpoints of two sides of a triangle is equal to the third side.
- The length of the line segment joining the midpoints of two sides of a triangle equals

In the opposite figure:

If
$$ED = 8 \text{ cm}$$
.

14



Page [11] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [3] - Mr. Mahmoud

[C]: Essay Problems: -

Prove that: the ray drawn from the midpoint of a side of a triangle parallel to another side bisects the third side.

2018 Exam (4) Question (3)(a)

In the oposite figure:

$$\overrightarrow{DE} // \overrightarrow{BC}$$
, m ($\angle DAB$) = 82°

and m (\angle D) = 32°

2

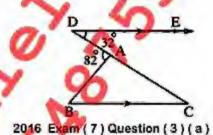
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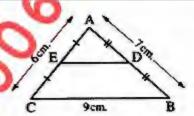
Find by proof: $m (\angle B)$



In the opposite figure:

ABC is a triangle in which D and E are the midpoints of \overline{AB} and \overline{AC} respectively AB = 7 cm., BC = 9 cm.

and AC = 6 cm. Find: the perimeter of \triangle ADE



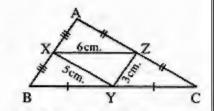
2016 Exam (11) Question (3)(b)

In the opposite figure:

X, Y, Z are the midpoints of AB, BC, CA respectively.

If XY = 5 cm., YZ = 3 cm, and XZ = 6 cm.

Find with proof the perimeter of Δ ABC

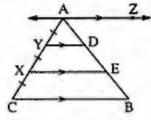


2018 Exam (6) Question (3) (b)

In the opposite figure

AY = YX = XC and AB = 12 cm.

Find: the length of AD



2016 Exam (9) Question (5)(a)

In the opposite figure:

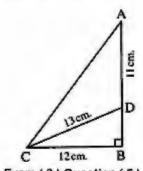
ABC is a triangle in which

$$m (\angle B) = 90^{\circ}$$

 $D \in \overline{AB}$ such that AD = 11 cm.

If BC = 12 cm. , DC = 13 cm. ,

find : the length of each of BD and AC



2016 Exam (3) Question (5)(a)

Page [13] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [3] - Mr. Mahmoud

		2018 Exam (5) Question (4)(a)
13	In the opposite figure : $\overrightarrow{DE} // \overrightarrow{CB}$, $m (\angle D) = 60^{\circ}$, $m (\angle C) = 50^{\circ}$ Find : $m (\angle DAC)$	D E 50 A 60 B 2016 Exam (6) Question (4) (b)
14	In the opposite figure: ABC is a triangle in which D, E and F are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively. BC = 12 cm., and AC = 10 cm. Find: the perimeter of the quadrilateral DECF	2018 Exam (14) Question (5) (a)
15	In the opposite figure: AB = 10 cm., BC = 16 cm., and AC = 14 cm., D, E and F are the midpoints of AB, BC, and AC respectively. Prove that: The perimeter of Δ DEF = 20 cm.	F D D B 2018 Exam (1) Question (3) (b)
16	In the opposite figure: $AC = BC \text{ in the triangle ABC}, E \text{ is the midpoint of } \overline{AB},$ $\overline{EF} // \overline{AC}, H \text{ and } G \text{ are the midpoints of } \overline{BD},$ $\overline{CD} \text{ respectively}$ $Prove \text{ that : } EF = GH = BF$	D H B G F E A 2016 Exam (1) Question (5) (b)
17	In the opposite figure : $m (\angle A) = m (\angle B) = 25^{\circ}$ Find : $m (\angle ACD)$	A 25° D C B el 2018 Exam (1) Question (3) (a

Homework

[A]: Choose The Correct Answer:

4	The number of axis of symmetry of a square equal	
	(a) 0 (b) 1 (c) 2 (d) 4	
2	The parallelogram whose diagonals are perpendicular to each other and not equal in length is called	
3	The rectangle of perpendicular diagonals is	
4	The hexagon has sides. (a) 5 (b) 6 (c) 7 (d) 8	
5	The edge length of a cube whose total area is 600 cm ² . is	
6	The measure of the right angle =	
7	In \triangle ABC, if D and E are the midpoints of AB and AC respectively, BC = 8 cm., then DE =cm. (a) 16 (b) 8 (c) 4 (d) 2	
8	The measure of the exterior angle of the equilateral triangle =	
9	The diagonal of square divided its vertex angle in two angles of the measure of each of them is	
10	In a parallelogram if the adjacent sides are equal in the length, then the shape is	
11	If ABCD is a parallelogram \Rightarrow then m (\angle A) = m (\angle	
12	The diagonal of the square makes an angle of measure with any of its sides. (a) 60° (b) 45° (c) 120° (d) 90°	
13	The sum of the measures of the accumulative angles at a point =	
14	The angle whose measure 90° is angle. (a) acute (b) right (c) obtuse (d) straight	

	Page [16] - Math	Mr. Mahmoud E	smaiel - Mobile : 01	006487539 - 01110882717
15	If X and Y are the mi	cm.	d AC in ∆ ABC and	3 XY = 3 cm.
	(a) 3	(b) 5	(c) 6	(d)9
16	Any triangle has at le (a) right	ast two(b) obtuse	interior angles. (c) acute	(d) reflex
17	The perimeter of a so	uare with side ler (b) 36	ngth 6 cm. = (c) 24	···· cm.
18	In Δ ABC if: m (∠ A	. ,	. ,	
19	In Δ ABC if: X, Y ar		AC and BC respect	(d) CY
20	* The triangle contain		angles at least (c) right	(d) reflex
21	The area of square of (a) 9	side length 3 cm	iscm ² .	(d) 3
22	If ABCD is a rhombu (a) BD (b)			a) CD
23	ABCD is a parallelog (a) 30°	(b) 45°	(c) 60°	(d) 120°
24	(a) 5 (b) 6	0	c) 7	nterior angle of it is 120°? (d) 8
25	The sum of the measure $(a) (n-2)$ $(b) (n-2)$	-2) × 180°	angles of a polygor (c) 360°	of n sides is
26	The pentagon has (a) 3	4 (c)		
27	The smallest number (a) zero	of the acute angle (b) I	e in any triangle is (c) 2	(d) 3
28	The right-angled trial (a) 1		right angle. (c) 0	(d) 3
29	In the oppointe figure $m (\angle A) = m (\angle C)$, (a) 50° (c) 25°	x =°	(b) 130° (d) 180°	D B C
30	In △ ABC, if m (∠ C)			∠ B isotherwise

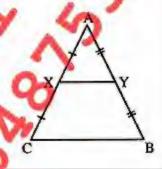
[B]: Complete the Following: -

The ray drawn parallel to one side of triangle and passing through the midpoint of another side

In the opposite figure:

XY //

2

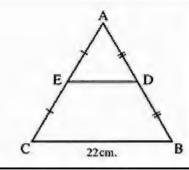


- 3 Every two vertically opposite angles are in measure.
- 4 The measure of each interior angle of the regular pentagon =
- 5 If ABCD is a parallelogram in which: $m(\angle A) = 120^{\circ}$, then $m(\angle B) = \dots$
- 6 The number of axes of symmetry of the rhombus is axes.
- The ray drawn from the midpoint of a side of a triangle parallel to another side the third side.

In the opposite figure:

If BC = 22 cm.

8



- If two straight lines intersect, then the measures of each two vertically opposite angles are
- Any triangle has at least two interior angles.
- 12 ABCD is parallelogram in which m (\angle A) = 100°, then m (\angle D) =°

	Page [18] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717
13	The two diagonals of the rhombus are
14	The measure of the exterior angle of a triangle is equal to the sum of
15	In the opposite figure: If ED = 8 cm. , then BC =
16	The two vertically opposite angles are
17	The sum of the measures of the angles of the quadrilateral equals
18	If ABCD is a parallelogram in which m ($\angle A$) = 80°, then m ($\angle B$) =
19	The rectangle is a parallelogram in which one of it's angles is
20	The measure of the exterior angle of any vertex of the equilateral triangle =°
21	The length of the line segment joining the midpoints of two sides of a triangle equals
22	The sum of the measures of the accumulative angles at a point is
23	The sum of the measures of the exterior angles of the convex polygon =
24	ABCD is a parallelogram in which m ($\angle A$) = 60°, then m ($\angle B$) =
25	If ABCD is rectangle and if AB = 4 cm., BD = 5 cm., then the area of the rectangle =
26	The measure of the exterior angle of a triangle is
27	The length of the line segment joining the midpoints of two sides of a triangle is equal to the third side.
28	The measure of the right angle =°
29	A circle its radius length 10 cm. , then its circumference = (Consider $\pi = 3.14$)

Page [18] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [3] - Mr. Mahmoud

[C]: Essay Problems: -

In the opposite figure:

 $\overrightarrow{DE} // \overrightarrow{YZ}$, m ($\angle ZDE$) = 50°

 $m (\angle YXZ) = 105^{\circ}$

1

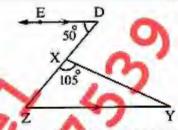
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Find: $m(\angle Z)$, $m(\angle Y)$, $m(\angle YXD)$



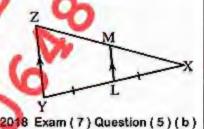
Model 2018 Exam (1) Question (4)(a)

In the opposite figure:

L is a midpoint of XY

 $,\overline{LM}//\overline{YZ},XZ=10$ cm.

Find: the length of XM



In the opposite figure:

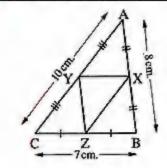
ABC is a triangle in which X, Y and Z are

midpoints of AB, AC and BC respectively.

AB = 8 cm., AC = 10 cm.

 $_{9}BC = 7 \text{ cm}.$

Find by proof: The perimeter of A XYZ



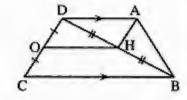
2017 Exam (7) Question (4)(a)

In the opposite figure

 $\overline{AD} // \overline{BC}$, $AD = \frac{1}{2} \overline{BC}$

, H and O are midpoints of DB and DC respectively

Prove that AHOD is a parallelogram



2018 Exam (2) Question (4) (a)

In the opposite figure:

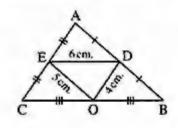
 \triangle ABC, in which D is the midpoint of \overline{AB} ,

E is the midpoint of AC,

O is the midpoint of BC,

ED = 6 cm. OD = 4 cm. and EO = 5 cm.

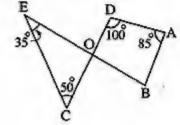
Find the perimeter of \triangle ABC



2016 Exam (9) Question (5) (b)

	Page [20] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006	6487539 - 01110882717
6	In the opposite figure : $\overrightarrow{DE} // \overrightarrow{BC}, m (\angle D) = 100^{\circ}$ $m (\angle C) = 30^{\circ} \text{ and } A \in \overrightarrow{DB}$ Find : $m (\angle BAC)$.	E D 100 A 2018 Exam (11) Question (4) (a)
7	In the opposite figure : ABCD is a parallelogram its diagonals are intersect at M , \overrightarrow{ME} // \overrightarrow{AB} prove that BE = EC	D A A M B B 2018 Exam (4) Question (3) (b)
8	In the opposite figure : $\overline{BA} / / \overline{CD}$, m ($\angle B$) = 50° and m ($\angle D$) = 60° Find with proof : m ($\angle CED$)	A B E 50 D D 2016 Exam (4) Question (3)(a)
9	In the opposite figure: D and E are midpoints of \overrightarrow{AB} and \overrightarrow{AC} AB = 12 cm. BC = 18 cm. and AC = 16 cm. Find with proof: the perimeter of figure ECBD	A D T A D T
10	In the opposite figure: ABC is a triangle in which D \rightarrow E \rightarrow O are midpoints of \overline{AB} \rightarrow \overline{BC} \rightarrow \overline{AC} resectively \rightarrow \overline{DE} // \overline{AC} AB = 6 cm \rightarrow BC = 8 cm \rightarrow AC = 10 cm. Find with prove the perimeter of : \triangle EDO	2018 Exam (2) Question (3) (a)
11	Complete: The line segment joining the midpoints of two sides of a	triangle is 2017 Exam(1) Question(4)(a)
12	Prove that: The sum of the measures of the interior angle	s of a triangle is 180° 2016 Exam (11) Question (3)(a)

In the opposite figure: AD = DB, AE = EC, $\overline{AX} // \overline{BC}$ 13 $,\overrightarrow{DE}\cap\overrightarrow{XC}=\{Y\},$ prove that: Y is the midpoint of \overline{XC} 2018 Exam (12) Question (5)(a) In the opposite figure: \overline{EO} // \overline{CD} , m ($\angle E$) = 50° 14 $m(\angle C) = 30^{\circ}$ Find the measures of angles of \triangle ABC, m (\angle ABD) Model 2018 Exam (2) Question (5)(a) In the opposite figure: D is the midpoint of AB, E is the midpoint of AC , $\overline{DF} \cap \overline{BC} = \{X\}$, DX = XF and BC = 12 cm. 15 Find: the length of XY 2018 Exam (13) Question (4)(a) In the opposite figure: $m (\angle A) = 85^{\circ}, m (\angle D) = 100^{\circ}$ $m (\angle C) = 50^{\circ} , m (\angle E) = 35^{\circ}$ 16 Find with proof each of: (1) m (Z DOB) (2) m $(\angle B)$



In the opposite figure:

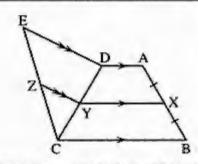
X is the midpoint of AB

,Y∈CD,Z€CE

17

, AD // XY // BC , YZ // DE

Is CZ = ZE? giving reason



2017 Exam (2) Question (4)(a)

Model 2018 Exam (2) Question (5) (b)

Prep [1] Ceometry-Second Term Unit [3]-Part [4]



Mr. Mahmoud Esmaiel 01006487539-01110882717

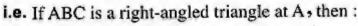
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Lesson [4]: Pythagoras Theorem

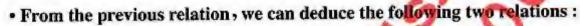
The sum of areas of the squares on the sides of the right angle of a right-angled triangle is the same as the area of the square on the hypotenuse.

We can also write the previous theorem as follows:

In a right-angled triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the other two sides.



$$(BC)^2 = (AB)^2 + (AC)^2$$



$$(AB)^2 = (BC)^2 - (AC)^2$$

$$(AB)^2 = (BC)^2 - (AC)^2$$
 $(AC)^2 = (BC)^2 - (AB)^2$

Remark [1]

You can get three numbers representing the lengths of sides of a right-angled triangle as follows:

- If M is an even number bigger than 2, then the numbers $M_1 \left(\frac{M}{2}\right)^2 1_2 \left(\frac{M}{2}\right)^2 + 1_3$
- If M is an odd number bigger than 2, then the numbers M_1 , $\frac{M^2-1}{2}$, $\frac{M^2+1}{2}$ represent three lengths of sides of a right-angled triangle as shown in the following table :

For Example:

in
$$\triangle$$
 ABC , AB = 3 cm , BC = 4 cm , m \angle (B) = 90 , AC = $\sqrt{(AB)^2 + (BC)^2}$ = 5 cm in \triangle ABC , AB = 6 cm , BC = 8 cm , m \angle (B) = 90 , AC = $\sqrt{(AB)^2 + (BC)^2}$ = 10 cm in \triangle ABC , AC = 15 cm , BC = 12 cm , m \angle (B) = 90 , AB = $\sqrt{(AC)^2 - (BC)^2}$ = 9 cm in \triangle ABC , AC = 25 cm , BC = 20 cm , m \angle (B) = 90 , AB = $\sqrt{(AC)^2 - (BC)^2}$ = 15 cm in \triangle ABC , AC = 25 cm , AB = 15 cm , m \angle (B) = 90 , BC = $\sqrt{(AC)^2 - (AB)^2}$ = 20 cm in \triangle ABC , AC = 10 cm , AB = 6 cm , m \angle (B) = 90 , BC = $\sqrt{(AC)^2 - (AB)^2}$ = 8 cm



Examples:

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ABCD is a rectangle in which $AB = 6$ cm.	AC = 10 cm.
---	--------------

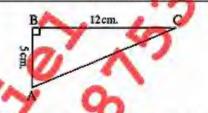
Find: The length of AD

2017 Exam (9) Question (3) (b)

In the opposite figure :

ABC is a triangle in which m (\angle B) = 90° AB = 5 cm. BC = 12 cm.

Find : AC



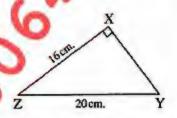
2017 Exam (1) Question (5) (a)

In the opposite figure:

XYZ is a triangle in which m ($\angle X$) = 90°

, YZ = 20 cm., XZ = 16 cm.

Find: The length of XY



2017 Exam (6) Question (4) (a)

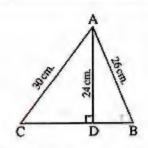
In the opposite figure:

ABC is a triangle in which: AD ⊥ B€

If AD = 24 cm., AB = 26 cm.

and AC = 30 cm.

Find: BC



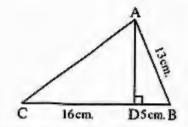
2017 Exam (4) Question (4)(b)

In the opposite figure

 $\overline{AD} \perp \overline{BC}$, BD = 5 cm.,

DC = 16 cm. AB = 13 cm.

Find the length of : AD, AC



2015 Exam (5) Question (3)(b)

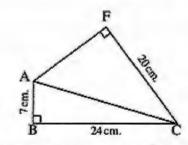
In the opposite figure:

ABCF is a quadrilateral in which:

 $m (\angle ABC) = m (\angle AFC) = 90^{\circ}$

AB = 7 cm, BC = 24 cm. FC = 20 cm.

Find : AC and AF



2017 Exam (11) Question (3) (b)

Solutions

to get the length of the rectangle >

In \triangle ABC: \cdots m (\angle B) = 90°

1 : $(BC)^2 = (AC)^2 - (AB)^2$

= 100 - 36 = 64

:. BC = $\sqrt{64}$ = 8 cm.

(The req.)

In \triangle ABC: \therefore (\angle B) = 90°

 $(AC)^2 = (AB)^2 + (BC)^2 = 25 + 144 = 169$

:. AC = $\sqrt{169}$ = 13 cm.

(the req.)

In $\triangle XYZ$: \therefore m ($\angle X$) = 90°

 $\therefore (XY)^2 = (YZ)^2 - (XZ)^2 = (20)^2 - (16)^2 = 144$

 $XY = \sqrt{144} = 12 \text{ cm}.$

(The req.)

In \triangle ABD: \therefore $\overrightarrow{AD} \perp \overrightarrow{BC}$ \therefore m (\angle ADB) = 90°

 $\therefore (BD)^2 = (AB)^2 - (AD)^2 = (26)^2 - (24)^2 = 100$

∴ BD = $\sqrt{100}$ = 10 cm.

4 In \triangle ACD: \because m (\angle ADC) = 90°

 $\therefore (CD)^2 = (AC)^2 - (AD)^2 = (30)^2 - (24)^2 = 324$

 \therefore CD = $\sqrt{324}$ = 18 cm.

 \therefore BC = BD + CD = 10 + 18 = 28 cm. (The req.)

In \triangle ABD: :: m (\angle ADB) = 90°

 $\therefore (AD)^2 = (AB)^2 - (BD)^2 = (13)^2 - (5)^2 = 144$

: AD = $\sqrt{144}$ = 12 cm.

In Δ ADC: ∵ m (∠ ADC) = 90°

 $\therefore (AC)^2 = (AD)^2 + (CD)^2 = (12)^2 + (16)^2 = 400$

:. AC = $\sqrt{400}$ = 20 cm.

(The req.)

In \triangle ABC: \therefore m(\angle B) = 90°

 $\therefore (AC)^2 = (AB)^2 + (BC)^2 = (7)^2 + (24)^2 = 625$

∴ AC = $\sqrt{625}$ = 25 cm.

 \rightarrow In \triangle AFC: $m (\angle F) = 90^{\circ}$

 $\therefore (AF)^2 = (AC)^2 - (FC)^2 = (25)^2 - (20)^2 = 225$

∴ AF = $\sqrt{225}$ = 15 cm.

(the req.)

In \triangle BCD: \therefore m (\angle B) = 90°

 $(BD)^2 = (DC)^2 - (BC)^2 = 169 - 144 = 25$

∴ BD = $\sqrt{25}$ = 5 cm.

 $7 \therefore AB = 5 + 11 = 16 \text{ cm}.$

In \triangle ABC: \because m (\angle B) = 90

 $(AC)^2 = (AB)^2 + (BC)^2 = 256 + 144 = 400$

 $\therefore AC = \sqrt{400} = 20 \text{ cm}$

(The reg.)

In \triangle ABC : $m(\angle B) = 90^{\circ}$

 $(AB)^2 = (AC)^2 - (BC)^2 = 289 - 64 = 225$

 $\therefore AB = \sqrt{225} = 15 \text{ cm}.$

AD = AB - DB = 15 - 3 = 12 cm.

 $8 \longrightarrow AE = 2BC \longrightarrow AE = 2 \times 8 = 16 \text{ cm}.$

AE // BC > AB is a transversal

 \therefore m (\angle A) = m (\angle B) = 90° (alternate angles)

 $\therefore (ED)^2 = (AD)^2 + (AE)^2 = 144 + 256 = 400$

 $ED = \sqrt{400} = 20 \text{ cm}.$

(The req.)

: The length = $\frac{48}{6}$ = 8 cm.

9 . The length of diagonal = $\sqrt{8^2 + 6^2}$ = 10 cm.

(The req.)

ABFD is a rectangle

 \therefore DF = AB = 12 cm.

AD = BE = 16 cm.

10 ∴ FC = 25 - 16 = 9 cm.

 $_{2}$ \simeq m (\angle DFC) = 90°

 $(DC)^2 = (DF)^2 + (FC)^2 = 144 + 81 = 225$

.. DC = $\sqrt{225}$ = 15 cm.

(The req.)

Construction : Draw DE 1 BC

Proof: ABED is a rectangle

 \therefore DE = AB = 12 cm.

 $_{2}$ AD = BE = 16 cm.

EC = 25 - 16 = 9 cm.

• ∵ m (∠ DEC) = 90°

 $(DC)^2 = (DE)^2 + (EC)^2 = 144 + 81 = 225$

 \therefore DC = $\sqrt{225}$ = 15 cm.

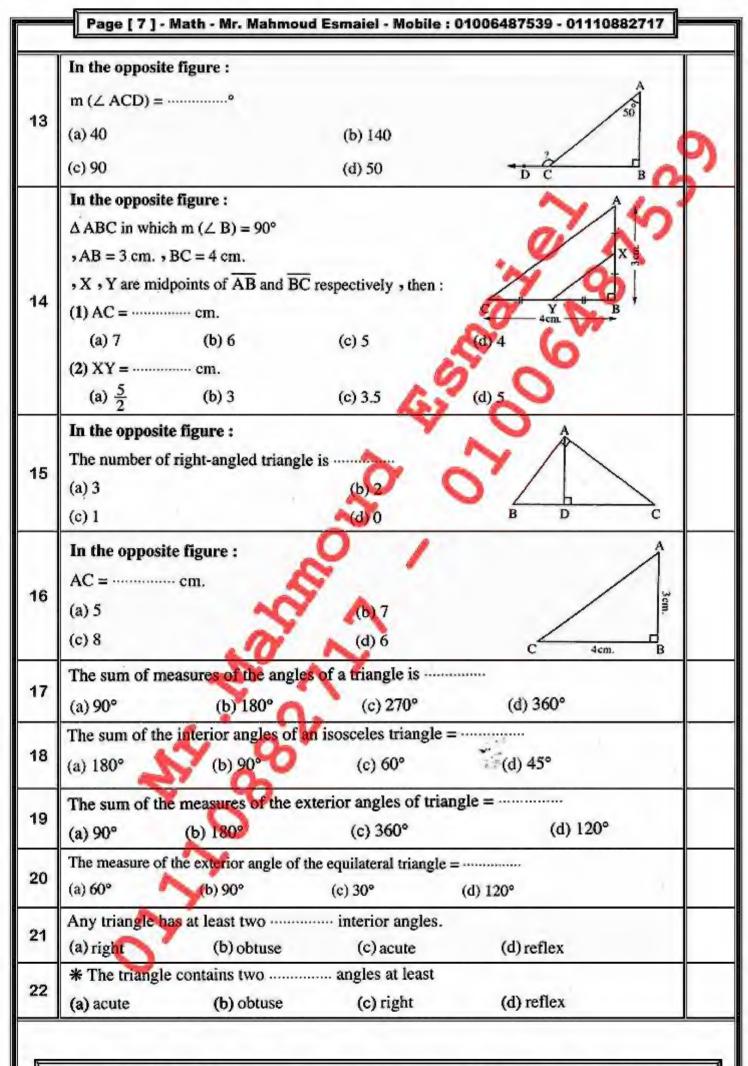
(The req.)

Exercises

[A]: Choose The Correct Answer:

1	In \triangle ABC if m (\angle A) = m (\angle B) + m (\angle C), then m (\angle A) =
2	In \triangle ABC, if m (\angle A) + m (\angle C) = m (\angle B), then m (\angle B) =
3	In \triangle ABC, if m (\angle A) = m (\angle B) + m (\angle C), then m (\angle C)
4	\triangle ABC in which m (\angle A) = 90°, then (AC) ² = (BC) ² (AB) ² (a) + (b) × (c) - (d) ÷
5	If \triangle ABC is right angled at B, then $(AB)^2 = \cdots$ (a) $(AC)^2 + (BC)^2$ (b) $(AC)^2 - (BC)^2$ (c) $(BC)^2 - (AC)^2$ (d) $(AC) - (BC)$
6	In \triangle ABC if m (\angle B) = 90°, AB = 6 cm., BC = 8 cm., then AC =
7	In \triangle ABC, if m (\angle B) = 90°, AB = 3 cm., BC = 4 cm., then AC = cm. (a) 7 (b) 1 (c) 5 (d) 4
8	In \triangle ABC, if m (\angle B) = 90°, AC = 10 cm. and BC = 8 cm. , then AB = cm. (a) 36 (b) $\sqrt{164}$ (c) 6 (d) 8
9	In \triangle ABC, if m (\angle B) = 90°, AB = 5 cm., AC = 13 cm., then BC = cm. (a) 8 (b) 10 (c) 12 (d) 18
10	In \triangle ABC, if m (\triangle A) = 90°, BC = 25 cm. and AC = 20 cm., then AB =cm. (a) 20 (b) 25 (c) 10 (d) 15
11	ABC is a right-angled triangle at B, if AC = 41 cm. and BC = 40 cm. then AB =
12	In the opposite figure: AC =

3cm.



[B]: Complete the Following: -

- 1 In \triangle ABC, if m (\angle A) = 90°, then (BC)² =
- 3 If ABC is a right-angled triangle at B, then $(BC)^2 = \dots$
- 4 If ABC is right-angled triangle at B, then $(AB)^2 = (AC)^2$
- 5 In $\triangle XYZ$, m ($\angle Y$) = 90°, then $(XZ)^2$ =
- 6 In \triangle XYZ if m (\angle Y) = 90°, then (XZ)² =
- 7 In \triangle ABC, if m (\angle A) = 90°, then (BC)² = (AB)² +
- 8 If $(AC)^2 = (AB)^2 (BC)^2$, then the measure of angle (...) = 90°
- 9 If XYZL is a rectangle, then $(XY)^2 + (YZ)^2 = (\dots)^2$
- 10 In the rectangle ABCD, $(AB)^2 + (AD)^2 = \dots$
- 12 Area of a triangle =
- In the right-angled triangle the area of the square on equals the sum of areas of the squares on the other two sides.
- In the right-angled triangle, area of the square drawn on the hypotenuse equals of the lengths of the other two sides.
- In the right-angled triangle, area of the square drawn on the hypotenuse equals
- 16 If Δ ABC is a right-angled triangle at A, then the longest side is called

	Page [9] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717
17	If \triangle ABC is a right-angled triangle at B, AB = 6 cm., BC = 8 cm., then AC =
18	In \triangle ABC, if m (\angle B) = 90°, AB = 3 cm. and BC = 4 cm., then AC =
19	The length of diagonal of a rectangle whose dimensions are 6 cm. and 8 cm. =
20	If \triangle XYZ is a right angled triangle at X \Rightarrow XY = 12 cm. and XZ = 9 cm. , then YZ =
21	If ABC is a right-angled triangle at B, AB = 20 cm; and AC = 25 cm., then BC = cm.
22	In the opposite figure : AC = cm.
23	In the opposite figure : BC =
24) In the opposite figure : AC = cm. B 4cm. C
25	In the opposite figure: The value of X =
26	If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
27	A circle its radius length 10 cm., then its circumference = (Consider $\pi = 3.14$)

Page [9] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [4] - Mr. Mahmoud

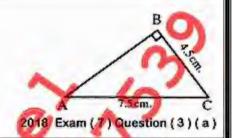
[C]: Essay Problems: -

In the opposite figure:

ABC is a right-angled triangle at B

AC = 7.5 cm. BC = 4.5 cm.

Find: the length of AB



In the opposite figure:

AB = 7 cm., CB = 24 cm.

and DC = 20 cm.

4

2

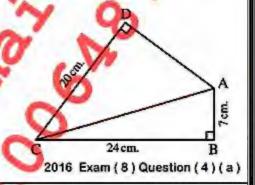
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Find: (1) The length of AC

(2) The length of AD



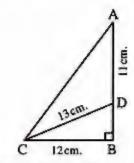
In the opposite figure:

 \triangle ABC in which m (\angle B) = 90°

 $D \in \overline{AB}$ such that AD = 11 cm.

, if BC = 12 cm, DC = 13 cm

Find the length of each of : AB, AC



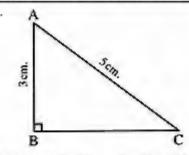
2018 Exam (10) Question (4)(a)

ABC is a right-angled triangle at B

If AB = 3 cm.

, AC = 5 cm.

Find: the length of BC



2018 Exam (15) Question (3) (b)

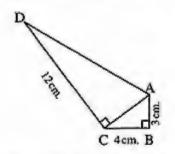
In the opposite figure:

 $m (\angle B) = m (\angle ACD) = 90^{\circ}$

, AB = 3 cm. , BC = 4 cm.

, CD = 12 cm.

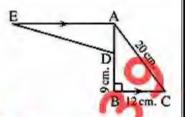
Find: The length of each of AC and AD



2017 Exam (7) Question (5)(a)

In the opposite figure:

 \triangle ABC in which m (\angle B) = 90°, \overline{AE} // \overline{BC} if BC = 12 cm., AC = 20 cm., $D \in \overline{AB}$ such that BD = 9 cm., AE = 2 BC



Find:

- 1) The length of \overline{AD}
- (2) The length of ED

2018 Exam (13) Question (5) (a)

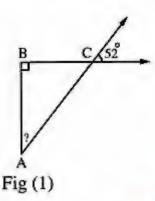
In the following figures, find the measure of the angle marked by (?)

7

8

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6





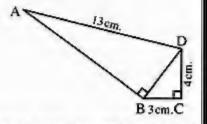
2018 Exam (15) Question (5) (a)

In the opposite figure:

BC = 3 cm., CD = 4 cm., DA = 13 cm

 $m (\angle ABD) = m (\angle C) = 90^{\circ}$

Find with proof the length of : BD , AB



2018 Exam (6) Question (5) (b)

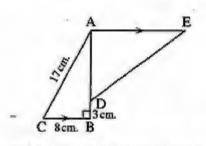
In the opposite figure:

 \triangle ABC in which m (\angle B) = 90°, \overline{AE} // \overline{BC}

, if BC = 8 cm., AC = 17 cm.

 $D \in AB : BD = 3 \text{ cm}$, AE = 2 BC

Find: The length of each of AD and ED



2017 Exam (8) Question (3)(a)

Complete:

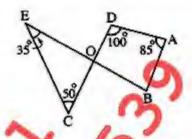
In the opposite figure:

$$\overline{DC} \cap \overline{BE} = \{O\}$$
, $m (\angle A) = 85^{\circ}$,

$$m (\angle D) = 100^{\circ}$$
, $m (\angle E) = 35^{\circ}$ and

$$m(\angle C) = 50^{\circ}$$

Find with proof: $m (\angle B)$



2016 Exam (2) Question (3)(a)

In the opposite proof:

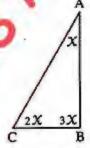
Find with proof: the measures of the angles of \triangle ABC

12

13

14

11



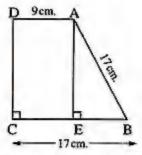
2016 Exam (15) Question (5) (b)

In the opposite figure:

ABCD is a trapezium, where $\overline{AD} // \overline{BC}$, m ($\angle DCB$) = 90°, $\overline{AE} \perp \overline{BC}$ and $\overline{AB} = BC = 17$ cm., $\overline{AD} = 9$ cm.

Find: 1 The length of DC

(2) The area of the trapezium ABCD



2017 Exam (15) Question (5)(a)

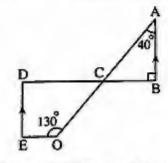
In the opposite figure:

$$\overline{BD} \cap \overline{AO} = \{C\}, \overline{AB} / / \overline{DE}$$

$$m (\angle A) = 40^{\circ} \cdot m (\angle B) = 90^{\circ}$$

and m (∠ COE) > 130°

Find: m(ZE)



2016 Exam (15) Question (4) (b)

Homework

[A]: Choose The Correct Answer:

- - (a) 180°
- $(b) 45^{\circ}$
- (c) 90°
- (d) 120°
- If \triangle ABC is right angled at B, then $(AB)^2 = \cdots$
- 2 (a) $(AC)^2 + (BC)^2$

(b) $(AC)^2 - (BC)^2$

(c) $(BC)^2 - (AC)^2$

- (d)(AC)-(BC)
- In \triangle ABC, if m (\angle A) = 90°, BC = 25 cm. and AC = 20 cm., then AB \Rightarrowcm.
- 3 (a) 20

4

- (b) 25
- (c) 10
- (d) 15

In the opposite figure:

 \triangle ABC in which m (\angle B) = 90°

AB = 3 cm. BC = 4 cm.

, X , Y are midpoints of AB and BC respectively , then :



- (a) 7
- (b) 6
- (c) 5
- (d)4

- (2) XY = cm.
 - (a) $\frac{5}{2}$
- (b) 3
- (c) 3.5
- (d) 5
- The measure of the exterior angle of the equilateral triangle =
- (a) 60°
- (b) 90°
- (c) 30°
- (d) 120°
- Any triangle has at least two angles.
- 6 (a) reflex
- (b) obtuse
- (c) acute
- (d) right
- If X and Y are the midpoints of \overline{AB} and \overline{AC} in $\triangle ABC$ and $\overline{XY} = 3$ cm.
- 7 then BC = cm.
 - (a) 3
- (b) 5
- (c) 6
- (d)9
- Δ ABC in which m (Δ A) = 90°, then $(AC)^2 = (BC)^2$(AB)²
 - (a)
- (b) x
- (c) -
- (d) ÷
- In \triangle ABC, if m (\angle B) = 90°, AB = 5 cm., AC = 13 cm., then BC =cm.
- 9 (a) 8
- (b) 10
- (c) 12
- (d) 18
- The sum of the measures of the exterior angles of triangle =
- 10 (a) 90°
- (b) 180°
- (c) 360°

- (d) 120°
- The smallest number of the acute angle in any triangle is
- 11 (a) zero
- (b) I
- (c) 2
- (d) 3

	Page [14] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717
12	In \triangle ABC, if D and E are the midpoints of \overrightarrow{AB} and \overrightarrow{AC} respectively, BC = 8 cm., then DE = cm.
13	(a) 16 (b) 8 (c) 4 (d) 2 In \triangle ABC, if m (\angle A) = m (\angle B) + m (\angle C), then m (\angle C)
14	In \triangle ABC, if m (\angle B) = 90°, AC = 10 cm. and BC = 8 cm., then AB = cm. (a) 36 (b) $\sqrt{164}$ (c) 6
15	In the opposite figure: AC =
16	The sum of the interior angles of an isosceles triangle = (d) 45° (a) 180° (b) 90° (c) 60° (d) 45°
17	The right-angled triangle has right angle. (a) 1 (b) 2 (c) 0 (d) 3
18	The line segment joining the midpoints of two sides of a triangle is the third side. (a) perpendicular to (b) equal to (c) parallel to (d) bisect to
19	In \triangle ABC, if m (\angle C): m (\angle A): m (\triangle B) = 1:2:4, then \angle B is
20	In \triangle ABC, if m (\angle A) \neq m (\angle C) = m (\angle B), then m (\angle B) =
21	In \triangle ABC, if m (\angle B) = 90° , AB = 3 cm., BC = 4 cm., then AC = cm. (a) 7 (b) 1 (c) 5 (d) 4
22	In the opposite figure: AC =
23	The sum of measures of the angles of a triangle is
24	* The triangle contains two

[B]: Complete the Following: -

- 1 In \triangle ABC, if m (\angle A) = 90°, then (BC)² =
- 2 If \triangle XYZ is a right angled triangle at X, XY = 12 cm. and XZ = 9 cm., then YZ = \square
- 3 If ABC is right-angled triangle at B, then $(AB)^2 = (AC)^2 \frac{1}{2}$
- 4 The sum of the measures of the angles of the quadrilateral equals
- In the right-angled triangle, the area of the square on equals the sum of areas of the squares on the other two sides.
- 6 ABCD is parallelogram in which m (∠ A) = 100°, then m (∠ D) =°
- 8 In the parallelogram XYZL, if m $(\triangle X) = \frac{1}{2}$ m $(\triangle Y)$, then m $(\triangle Y) = \dots$ °
- If a straight line intersects two parallel straight lines, then every two interior angles in the same side of the transversal are
- 10 In the right-angled triangle, area of the square drawn on the hypotenuse equals
- 11 ABCD is a parallelogram in which m (∠ A) = 130°, then m (∠ B) =°
- 12 If $(AC)^2 = (AB)^2 (BC)^2$, then the measure of angle (.....) = 90°
- 13 Each two opposite angles in a parallelogram are
- 14 Area of a triangle =
- 15 If ABCD is a parallelogram in which m ($\angle A$) = 80°, then m ($\angle B$) =

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17	The measure of each interior angle of the regular pentagon =	
18	In the rectangle ABCD, $(AB)^2 + (AD)^2 = \dots$	
19	ABCD is a parallelogram in which m (\angle A) = 50°, then m (\angle B) =	
20	The length of diagonal of a rectangle whose dimensions are 6 cm. and 8 cm. = cm.	
21	If ABC is a right-angled triangle at B, then $(BC)^2 = \cdots$	
22	The sum of the measures of the exterior angles of the convex polygon	
23	In \triangle ABC \Rightarrow if m (\angle A) = 90° \Rightarrow then (BC) ² = (AB) ² \Rightarrow	
24	If two opposite sides in the quadrilateral are parallel, then it is called	
25	If Δ ABC is a right-angled triangle at A, then the longest side is called	
26	In the parallelogram XYZL, if $m(\angle X) = \frac{1}{3} m(\angle Y)$, then $m(\angle L) = \dots$	
27	In $\triangle XYZ$, m ($\triangle Y$) = 90°, then $(XZ)^2 = \cdots$	
28	The measure of each interior angle of the regular hexagon is°	
29	In the right-angled triangle, area of the square drawn on the hypotenuse equals of the lengths of the other two sides.	
30	If ABCD is a parallelogram in which: m (∠ A) = 120°, then m (∠ B) =°	
31	In \triangle ABC if in $(\angle B) = 90^{\circ}$, then $(AC)^2 = \cdots + \cdots$	
32	A circle its radius length 10 cm. , then its circumference = (Consider π = 3.14)	
33	If the measure of one angle of a triangle equals the sum of the measures of the other two angles, then the triangle is	
34	ABCD is a parallelogram in which m (\angle A) = 60°, then m (\angle B) =	

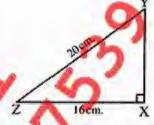
[C]: Essay Problems: -

In the opposite figure:

XYZ is right-angled triangle at X

YZ = 20 cm. XZ = 16 cm.

Find: the length of XY



2018 Exam (2) Question (5) (b)

In the opposite figure:

2

3

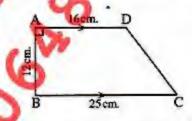
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5

ABCD is a quadrilateral in which m ($\angle A$) = 90°

AB = 12 cm. BC = 25 cm. AD = 16 cm. and AD # BC

Find with proof: The length of \overline{DC}



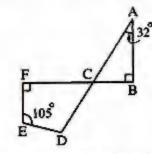
2017 Exam (10) Question (5) (b)

In the opposite figure:

 $\overline{AD} \cap \overline{FB} = \{C\}, m (\angle A) = 32^{\circ}$

 $m (\angle B) = m (\angle F) = 90^{\circ} \text{ and } m (\angle E) = 105^{\circ}$

Find: m (\(D \)



2016 Exam (7) Question (4) (b)

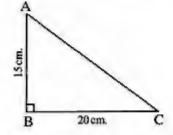
In the opposite figure :

 \triangle ABC in which m (\triangle B) = 90°

 $_{2}AB = 15$ cm.

, BC = 20 cm.

Find with proof: The length of \overline{AC}



2017 Exam (5) Question (4)(a)

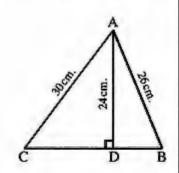
In the opposite figure:

 $\overline{AD} \perp \overline{BC}$, if $\overline{AD} = 24$ cm.

AB = 26 cm AC = 30 cm.

Find:

- (1) The length of BC
- ② The area of Δ ABC



2018 Exam (9) Question (4)(a)

Page [18] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [4] - Mr. Mahmoud

Page [19] - Prep. [1] - Second Term - Geometry - Unit [3] - Part [4] - Mr. Mahmoud

Prep [1] Ceometry-Second Term Unit [3]-Part [5]



Mr. Mahmoud Esmaiel 01006487539-01110882717

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Lesson [5]: Geometric Transformation

Prelude

Notice the changing which happened to the position of the letter E corresponding to its previous position directly in each case of the following cases:

The first case	E	11000	3		E	11111	3
The second case	E		E	1100	' E/		E
The third case	٠E	11100	П	1110	$g_{\exists_{\ell}}$	rigare)	Ш
The time odes	٠E	1110	Ш	unio	B.	Cisos)	П

- The geometric transformation in the first case is called: reflection
- The geometric transformation in the second case is called translation
- The geometric transformation in the third case is called rotation

The concept of the geometric transformation

In each of the following figures, notice the image of \triangle ABC and deduce what happened to it:

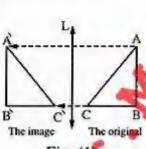


Fig. (1)

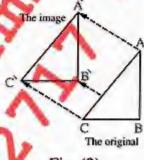


Fig. (2)

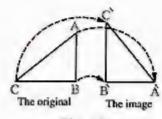


Fig. (3)

In each of the previous figures, notice that:

- The point A has been transferred to A
- The point B has been transferred to B
- The point C has been transferred to C

Thus, all the points of \triangle ABC have been transferred to another position, then we say that Δ ABC has been transformed from position to another position.

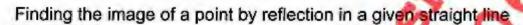
Geometric transformations have many types as: reflection, translation and rotation which we will study each of them in details in the following lessons.

Lesson [6]: Reflection

Definition of reflection in a straight line

Reflection in the straight line L maps each point A to the point \hat{A} in the same plane such that :

- If A∉L, then the straight line L is the perpendicular bisector to the line segment AA
- 2 If B ∈L, then B is reflected onto itself
 i.e. B coincides B



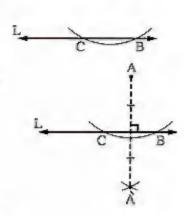
- To find A which is the image of A by reflection in the straight line L , we do as follows :
 - Draw an arc of a circle with centre A
 to cut L at B and C
 - With the same radius length taking B and C as centres, draw two arcs in the other side of the straight line L to intersect at A, then A is the image of A by reflection in L

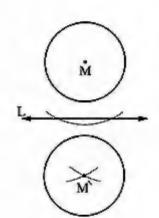
Check by measuring that

AA L and L bisects AA

Finding the image of a circle by reflection in a given straight line

- To find the image of a circle M by reflection in the straight line L,
 we do as follows:
 - Find the image of the centre M by reflection in L as we did before a say M
 - 2 Use the compasses with radius length equal to the radius length of the circle M to draw a circle with centre M that will be the image of the circle M by reflection in L



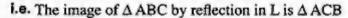


Symmetry

• In the opposite figure :

ABC is a triangle, $\overrightarrow{AD} \perp \overrightarrow{BC}$, D is the midpoint of \overrightarrow{BC} , we find that:

- The image of A by reflection in L is itself (A)
- The image of B by reflection in L is C
- The image of C by reflection in L is B



We can say that ABC is transformed to itself by reflection in the straight line L,

Therefore the straight line L is called the axis of symmetry of \triangle ABQ



If the reflection in a line transforms the figure to itself, then this line is called an axis of symmetry of the figure.

The axis of symmetry divides the figure into two congruent figures.

The axes of symmetry of some geometric figures

The figure	An isosceles triangle	An equilateral triangle	Scalene
Number of axes of symmetry	0	3	Zero (does not exist)
The figure	Parallelogram	Rectangle	Rhombus
Number of axes of symmetry	Zero (does not exist)	2	2
The figure	Square	Trapezium	An isosceles trapezium
Number of axes of symmetry	4	Zero (does not exist)	1

The figure

Number of axes of

symmetry

The circle



The regular hexagon

An infinite number

5

The regular pentagon

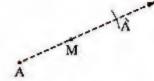
Definition of reflection in a point

Reflection in a point M maps each point A in the plane to the point A in the same plane where M is the midpoint of the line segment AA , the point M is called the centre of reflection and the image of M by reflection in M is itself.



Finding the image of a point by reflection in a given point

- To find the image of a point as A by reflection in M , we do as follows:
 - T Draw AM
 - 2 Using the compasses with open length equals MA, then use M as a centre and draw an arc to intersect AM at a point as A, then A is the image of the point A by reflection in the point M



From the previous, we found that: MA = MA

Lesson [7]: Translation

- i.e. To determine the new position of the car after its movement, we should know two important elements which are :
 - The magnitude of the translation (25 metres).
 - The direction of the translation (forward in a straight line).

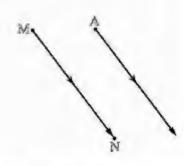
According to this, we can say that :

Translation is a geometrical transformation which maps each point A in the plane to another point A in the same plane with a constant distance in a certain direction.

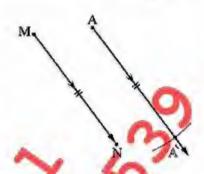
Translation in the plane

Finding the image of a point by a given translation

- To find A which is the image of A by translation MN in the direction of MN , we do as follows :
 - Draw from A a ray parallel to MN and in the same direction.

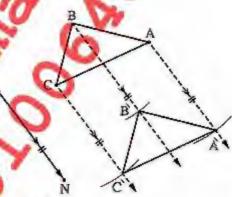


- 2 By the compasses in A as a centre with radius = MN, draw an arc to intersect the ray drawn from A at the point \hat{A} ($A\hat{A}$ = MN and $\overline{A\hat{A}}$ // \overline{MN})
- Then \hat{A} is the image of A by translation of magnitude MN in the direction of \overrightarrow{MN}



Finding the image of a polygon by a given translation

- To find the image of a polygon as \triangle ABC by translation MN in the direction of \overline{MN} , we do as follows:
 - Find the image of each vertex of the vertices of Δ ABC by translation MN in the direction of MN as we mentioned before (say A for A, B for B and C for C)
 - Draw AB, BC and CA then ΔABC is the image of ΔABC by translation MN in the direction of MN



Check that :

- AB = AB BC = BC and CA = CA
- $m(\angle A) = m(\angle A)$, $m(\angle B) = m(\angle B)$, $m(\angle C) = m(\angle C)$

From the previous, we deduce that translation is a geometrical transformation which maps the geometrical figure to another geometrical figure congruent to it.

Lesson [8]: Rotation

The concept of rotation

If M is a fixed point in the plane, then the rotation around M with an angle of measure θ is a geometric transformation transforming each point A in the plane to another point A in the same plane such that $m (\angle AMA) = \theta$, MA = MA It is denoted by $R(M, \theta)$ where :



- M is the centre of rotation.
- θ is the measure of the angle of rotation.

According to this concept, the rotation is determined completely if we know the following elements

- The centre of rotation.
- 2 The measure of the angle of rotation (θ)
- The direction of rotation.

Remark [1]

The measure of rotation angle is positive if the rotation is anticlockwise and it is negative if the rotation is clockwise.

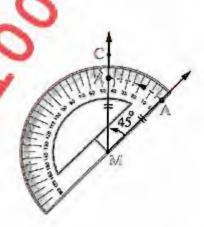


Rotation in the plane

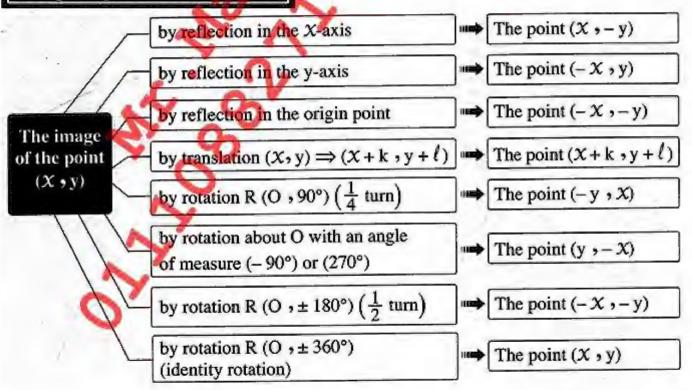
Finding the image of a given point by a given rotation

Firstly: Finding the image of the point A by rotation around the point M with an angle of measure 45° i.e. R (M , 45°):

- Draw the ray MA
- Put the protractor with its straight edge on MA
 and in the anticlockwise direction then draw
 MC such that m (∠ AMC) = 45°
- Use the compasses at the point M as a centre with radius = MA, draw an arc to cut MC at A then A is the image of the point A by rotation around M with an angle of measure 45°



Very Important Notes:



Examples:

3

4

5

7

8

Using the la	attice, draw ABC where A (1,0)) ,	B (0,2) and C (-3,1)
--------------	-------------------------------	------	----------------------

, then draw its image by reflection in X-axis.

2017 Exam (1) Question (5) (b)

Using the lattice, find the image of the triangle ABC by reflection in y-axis where
$$A(-1,2)$$
, $B(-5,5)$, $C(-6,3)$

2017 Exam (12) Question (3) (b)

Draw the triangle ABC in which AB = 3 cm. BC = 4 cm. AC = 5 cm.

, then draw its image by reflection in BC

2017 Exam (8) Question (5)(b)

Draw \triangle ABC in which AB = 3.5 cm. , m \angle A \angle 90° AC = 5 cm.

, then draw its image by reflection in AC

2017 Exam (9) Question (4) (a)

Using the square lattice, draw \triangle ABC where A (-2,3), B (2,3), C (2,6), then find the image of \triangle ABC by translation $(X, y) \longrightarrow (X+2, y-1)$

2017 Exam (13) Question (5) (b)

Draw the rectangle ABCD in which BC = 6 cm. and AB = 4 cm., draw the image of the rectangle ABCD by rotation R (A 190°)

2016 Exam (5) Question (5) (a)

In square lattice, draw \triangle ABC where A(0,6), B(-2,1), C(2,1)

, then find:

- (1) The image of Δ ABC by reflection in y-axis.
- (2) The image of \triangle ABC by rotation (0, 180°)

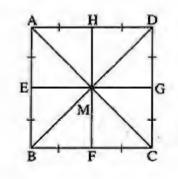
2017 Exam (6) Question (4)(b)

In the opposite figure:

ABCD is a square in which $E \cdot F \cdot G$ and H are midpoints of $\overrightarrow{AB} \cdot \overrightarrow{BC} \cdot \overrightarrow{CD}$ and \overrightarrow{AD} respectively

Find:

- 1) The image of Δ MGD by rotation at point M by angle with measure (-90°)
- ② The image of Δ MGD by reflection in EG
- (3) The image of Δ MGD by translation (DH) in direction \overline{DH}



Exercises

[A]: Choose The Correct Answer:

	In the opposite figure :
	The image of the point A by reflection
1	in the point M is
	(a) A (b) B
	(c) C (d) D
	The image of the point $(2, -5)$ by reflection in X -axis is
2	(a) (-2,5) (b) (2,5) (c) (-2,-5) (d) (5,2)
3	The image of the point (3, -5) by reflection in the y-axis is
,	(a) $(3,5)$ (b) $(-3,-5)$ (c) $(5,-3)$ (d) $(-3,5)$
4	The image of the point $(-1, 4)$ by the translation $(3, -2)$ is
	(a) (2,2) (b) (-2,-2) (c) (2,-2) (d) (-2,2)
	If the image of the point (3, -2) by rotation about the origin point is itself
5	then the measure of the rotation angle is
	The image of the point (-5,7) by rotation about the origin point with an angle of
6	measure 90° is
	(a) (-7,-5) (b) (5,-7) (c) (-7,5) (d) (7,5)
7	The image of the point (26-1) by reflection in the X-axis is
	(a) (2,1) (b) (1,2) (c) (-2,-1) (d) (-1,2)
8	The image of the point (2,5) by reflection in y-axis is
	(a) $(-2,5)$ (b) $(5,2)$ (c) $(-2,-5)$ (d) $(2,-5)$
	If the image of the point (-1,3) by a translation is (1,4), then the image of the
9	point $(3, -2)$ by the same translation is
	(a) $(1, 2)$ (b) $(5, -1)$ (c) $(-1, 2)$ (d) $(-2, -1)$
	If A $(4, -5)$ is the image of A by translation $(x, y) \longrightarrow (x-2, y+1)$ then the
10	point A =
	(a) (6,-4) (b) (4,-4) (c) (2,-4) (d) (6,-6)
44	The image of the point (4, 3) by rotation about the origin point with an angle of measure 90° is
11	(a) (4,3) (b) (-4,3) (c) (-3,4) (d) (-3,-4)
	(3)(-3)-4)

	Page [11] - Math - Mr. Mahmoud Esmaiel - Mobile : 01006487539 - 01110882717	
12	The image of the point $(1,5)$ by reflection in the \mathcal{X} -axis is	
13	The image of the point $(2, -1)$ by reflection in y-axis is	7)
14	The image of the point $(-1,3)$ by translation $(4,-2)$ is	
15	If the point $(a, -1)$ is the image of $(2, 4)$ by translation (x, y) — $(x + 1, y - b)$, then (a, b) is	
16	The image of the point $(3, -5)$ by rotation R $(0, 90^{\circ})$ is	
17	The image of the point $(-1,3)$ by reflection in $(-1,3)$ axis is	
18	The image of the point $(1, -4)$ by reflection in y-axis is	
19	The image of the point $(-1, 3)$ by translation $(x + 4, y - 2)$ is	
20	The image of the point $(5, -3)$ by translation 3 units in negative direction of x -axis is	
21	The image of the point $(2,3)$ by rotation about the origin point with an angle of measure 90° is (a) $(2,-3)$ (b) $(-2,3)$ (c) $(-3,2)$ (d) $(2,3)$	
22	The reflection in the X -axis maps the point B (X , y) to the point B (X , y) (a) (X , y) (b) (X , y) (c) (X , y) (d) (X , y)	
23	The image of the point $(-1, 3)$ by reflection in y-axis is	
24	The image of the point $(-1, 2)$ by translation of magnitude 3 units in the positive direction of y-axis is	
25	The image of the point $(5, -3)$ by translation $(1, 1)$ is	

[B]: Complete the Following: -

1	The image of the point (4, 1) by reflection in the origin point is
2	The reflection in the X-axis maps the point B (4, 2) to the point B
3	The translation is determined by and
4	The image of the point (4,6) by translation: $(x,y) \longrightarrow (x,y-7)$ is
5	The image of the point (X, y) by rotation about the origin point is itself, then the measure of rotation angle is
6	The image of the point (3, 2) by rotation with an angle of measure 180° about the origin is
7	The point $(3,7)$ is the image of the point by reflection in the x -axis.
8	The reflection in a line reserves ,
9	The image of the point (-4,5) by translation (2,-3) is
10	The neutral rotation maps the figure to
11	The image of the point (2, -3) by rotation about the origin point with an angle of measure 180° is
12	The image of the point $(3, 2)$ by reflection in the X -axis is
13	(-3,2) is the image of the point (3,2) by reflection in aixs.
14	The image of the point $(4, -5)$ by translation $(-2, 4)$ is
15	In the rotation around O with an angle of measure
16	(-3,2) is the image of the point (-3,-2) by reflection in

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17	The image of the point $(3, -5)$ by translation 3 units in the positive direction of x -axis is
18	Rotation in the plane reserves of angles.
19	The image of the point (3, -5) by rotation R (O, 90°) is
20	In the opposite figure: ABCD is a square, X, Y, Z, L are midpoints of its sides then: (1) The image of Δ AXO by reflection in XZ is
21	The image of the point $(2, -3)$ by reflection in X-axis is
22	The image of the point (3, -5) by reflection in the y-axis is
23	The image of the point $(3,5)$ by translation : (x,y) $(x+3,y-1)$ is
24	In the opposite figure The image of the triangle XBY by translation XZ in direction XZ is
25	The image of the point (3) 2) by rotation with an angle of measure 90° about the origin point is
26	The image of the point $C(X, y)$ is the point $\hat{C}(-X, -y)$ by rotation around the origin point O and an angle whose measure is
27	The image of the point (2, 1) by reflection in X-axis is
28	The image of the point (-3,5) by reflection in the y-axis is

[C]: Essay Problems: -

1	If the image of the point A by reflection in the χ -axis is $(2,3)$, locate the point A, then draw the image of A by reflection in the y-axis
	2016 Exam (1) Question (4)(a)
	On the orthogonal square lattice draw the triangle ABC where
2	A = (1, 1), $B = (3, 4)$ and $C = (5, 2)$, then draw the image of the triangle ABC
-	by rotation about the origin point with an angle of measure 90°
	2016 Exam (7) Question (5)(a)
	On the square lattice, draw AB where A (3, 2), B (-151)
3	then find its image by translation (-2, -5)
	2017 Exam (7) Question (3) (b)
	Draw \triangle ABC in which: AB = 5 cm., BC = 4 cm. and m (\angle B) = 90°
4	, then find the image of Δ ABC by reflection on AB
	2016 Exam (6) Question (3) (b)
5	Draw the image of triangle ABC where A(1, 1) , B(3, 4) , C(5, 2)
	by reflection in X-axis. Model 2018 Exam (2) Question (4) (a)
	Draw the rectangle ABCD in which BC = 6 cm, and AB = 4 cm., draw the image of
6	the rectangle ABCD by rotation R (A, 90°)
	2016 Exam (5) Question (5)(a)
	On a square lattice, draw AB where A(2,3) and B(4,1), then draw the image of AB
7	By rotation about the origin point with an angle of measure:
	(1) 90° (2) 180°
_	Light the agree letting down A.P. where A.(4, 2) and D.(1, 1), then Sandaha
8	Using the square lattice, draw AB where A $(4, 2)$ and B $(-1, -1)$, then find the
•	image of \overline{AB} by translation $(x, y) \longrightarrow (x + 2, y - 1)$
	Draw Δ ABC where A(1,5) , B(3,1) and C(5,3), then draw its image:
9	① By reflection in y-axis.
	(2) By rotation about origin point with an angle of measure 180° 2018 Exam (10) Question (5) (a)
	Draw the image of \triangle ABC in which: AB = 6 cm., BC = 4 cm., AC = 5 cm.
10	, by reflection in AC
	2018 Exam (12) Question (4) (b)
	On the square lattice, draw \triangle ABC where A(1,1), B(5,2), C(3,5)
11	then find its image by reflection in X-axis.
	2017 Exam (7) Question (4) (b)

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12	In the opposite figure: ABC is an equilateral triangle $X \cdot Y \cdot Z$ are the midpoints of $\overline{AB} \cdot \overline{AC}$ and \overline{BC} respectively Find the image of: (1) Δ_1 by reflection in \overline{XY} (2) Δ_2 by translation BZ in the direction of \overline{BZ} (3) Δ_2 rotation R (Z $\cdot -60^\circ$)
13	Draw the rectangle ABCD on a square lattice where A (0,0), B (0,2), C (4,2), D (4,0), then find its image by rotation about the origin point with an angle of measure 180° 2017 Exam (3) Question (4) (a)
14	On a square lattice, draw \triangle ABC, such that: A (4,4), B (4,2) and C (1,2) Find its image by translation $(x-2,y+1)$
15	In the opposite figure: Draw the image of the \triangle ABC by the reflection in the X -axis where A (2,2), C (6,4) and B (6,6) $x = \frac{10}{100} = \frac{2}{100} = \frac{3}{100} = \frac{1}{100} = \frac{1}{1$
16	Using the lattice, find the image of the triangle ABC by reflection in y-axis where $A(-1,2)$, $B(-5,5)$, $C(-6,3)$
17	In square lattice, draw Δ ABC where A (0,6), B (-2,1), C (2,1), then find: (1) The image of Δ ABC by reflection in y-axis. (2) The image of Δ ABC by rotation (0,180°) 2017 Exam (6) Question (4) (b)
18	On square lattice, draw the triangle whose vertices are A $(5,5)$, B $(5,3)$, C $(2,3)$, then determine each of the following: (1) The image of Δ ABC by translation $(-2,2)$ (2) The image of Δ ABC by reflection in y-axis.

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19	If the point A is the image of point B (-1,4) by refection in X-axis Find the image of A by translation (1,4)
20	In the square net draw \triangle ABC in which A (-2,2), B (3,1), and C (2,5), then find its image by reflection in the origin point.
21	In the opposite figure: ABCD is a square in which E, F, G and H are midpoints of AB, BC, CD and AD respectively Find: (1) The image of Δ MGD by rotation at point M by angle with measure (-90°) (2) The image of Δ MGD by reflection in EG (3) The image of Δ MGD by translation (DH) in direction DH 2017 Exam(10) Question(3)(a)
22	If the point A (4,5) is the image of the point A (1,7) by translation $(X,y) \longrightarrow (X+a,y+b) \text{ find :}$ ① The value of a and b ② The image of the point B (2, -4) by the same translation.
23	Complete: If the point $(1,4)$ is the image of the point $(-1,3)$ by a translation (x,y) , then the image of the point $(3,-2)$ by the same translation is
24	In the opposite figure: ABCD is a square, whose diagonals intersect at M Find: 1 The image of Δ ABC by reflection in AC 2 The image of Δ MAB by rotation about M with angle of measure (-90°) 2018 Exam (13) Question (5) (b)
25	On the lattice, find the image of the triangle LMN, where $L(-4,-1)$, $M(-1,-3)$, $N(0,-1)$ by reflection on the X-axis 2016 Exam (5) Question (3) (b)
	To the state of th

	Find \overrightarrow{AB} the translated image of \overrightarrow{AB} , where A (2, 1) and B (2,4) when translated
27	MN units in the direction of \overrightarrow{MN} , where M (-2,5)	and N (3,7) 2018 Exam (1) Question (3) (
	In the opposite figure :	. 0
	ABCD is a square of side length 6 cm.	D E
	and the origin point is its centre.	L M
28	Find:	. 0 9
20	① The image of Δ AΘM by translation 3 cm.	7 9
	in the direction of AB	O N N B
	(2) The image of Δ AOM by rotation R (O , 90°)	6
	(3) The image of Δ AOM by reflection in EN	2018 Exam (8) Question (4) (
	Using the square lattice, draw the triangle ABC when	
29	and C (-2,4), then draw its image by rotation R (0	> 180°) 2018 Exam (9) Question (3) (
	In the opposite figure :	A 9cm. B
	ABED is a trapezium in which AB // DE	\3
ы	$, m (\angle D) = 90^{\circ}, \overline{BC} \perp \overline{DE}$	/3
30	, BE = DE = 17 cm. , AB = 9 cm.	D C E
	Find: 1 The length of AD	
	(2) The image of AB by translation of magnitude AI	D in direction of AD 2017 Exam (13) Question (4) (
	Draw Δ ABC and draw its image by reflection in y-	
31	A(-6,-1) $B(-2,-1)$ $C(-5,-6)$	2017 Exam (4) Question (5) (
	In the opposite figure :	D A
	ABCD is a square whose diagonal	
32	intersect at M • find;	
	1 The image of A ABC by reflection in AC	M
	② The image of Δ MAB by reflection in point M	• C
	On a square lattice, draw the triangle ABC where A (2018 Exam (10) Question (3) (4,4), B(4,2), C(1,2
33	, then find its image by rotation about the origin point	with an angle of measure 180° 2018 Exam (15) Question (5) (

Homework

[A]: Choose The Correct Answer:

4	The image of the square by rotation about the origin point with an angle of measure 90° is				
	(a) rectangle. (b) square. (c) rhombus. (d) trapezium.				
	The point whose image by reflection in the origin point is itself is				
2	(a) (1,0) (b) (0,1) (c) (0,0) (d) (-1,0)				
3	The image of the point $(-2,3)$ by refletion in the y-axis is the point $(-3,2)$ (c) $(-3,2)$ (d) $(-3,-2)$				
4	The image of the point $(-1, 2)$ by translation of magnitude of 3 units in the positive direction of the \mathcal{X} -axis is				
	(a) (-1,5) (b) (2,2) (c) (-2,2) (d) (-1,3) The image of the point (-4,5) by translation (2,-3) is				
5	(a) (2,2) (b) (-2,2) (c) (2,-2) (d) (-2,-2)				
	The equivalent rotation to R (O, 90°) is R (O,)				
6	(a) -90 (b) 270 (c) 180 (d) -270				
-	The image of the point (-2,1) by reflection in the origin point is				
7	(a) $(2,1)$ (b) $(-2,1)$ (c) $(2,-1)$ (d) $(-2,-1)$				
0	The image of the point by reflection in y-axis is (3, 2)				
8	(a) (3,-2) (b) (-3,-2) (c) (-3,2) (d) (-2,3)				
9	The image of the point $(1, -2)$ by translation $(x, y) \longrightarrow (x-1, y+3)$ is				
9	(a) $(2,-5)$ (b) $(0,-1)$ (c) $(0,1)$ (d) $(2,5)$				
	The image of the point $(-4,3)$ by geometric transformation $(x,y) \longrightarrow (-x,y-7)$				
10	is				
	(a) (-4,-4) (b) (4,-4) (c) (4,10) (d) (-4,10)				
11	The image of the point (2 1,4) by rotation R (O, 180°) is				
	(a) (-1,-4) (b) (1,-4) (c) (4,1) (d) (1,4)				
12	The image of the point (3, -7) by reflection in the origin point is				
	(a) $(-3,7)$ (b) $(-3,-7)$ (c) $(3,-7)$ (d) $(3,7)$				
13	If the image of the point (9, -4) by rotation about the origin point is itself, then the measure of the rotation angle is				
13	(a) 90° (b) 180° (c) 270° (d) 360°				

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14	The image of the point $(-3, 2)$ by reflection in y-axis is	
15	The image of a rhombus by any translation is a)
16	The image of the point $(3, -2)$ by translation $(-1, 6)$ is	
17	The image of a triangle by rotation around the origin point with an angle of measure 180° is	
18	If \hat{A} is the image of A by reflection in M and MA = 6 cm., then $\hat{AA} = \cdots \cdot \cdot$	
19	The image of the point $(5, 1)$ by reflection in the origin point is	
20	The image of the point $(-3, 4)$ by reflection in the y-axis is	
21	The image of the square by any translation is a	
22	The image of the point $(3, -2)$ by translation $(-1, 4)$ is	
23	The image of a triangle by rotation about the origin point with an angle of measure 360° is	
24	In the opposite figure: Δ ABC is the image of Δ ABC by rotation about A with angle of measure (a) 30° (b) 80° (c) 110° (d) 140°	
25	The reflected image of the point A $(-3, 2)$ in the origin point is the point \overrightarrow{A} () (a) $(3, -2)$ (b) $(3, 2)$ (c) $(-3, -2)$ (d) $(2, -3)$	
26	The image of the point $(-3, 2)$ by reflection on the X-axis is	
27	The image of the point $(3, 5)$ by reflection in y-axis is	

[B]: Complete the Following: -

L	
1	If \hat{A} is the image of A by reflection in M and MA = 6 cm., then $\hat{A}\hat{A}$ =
2	The image of the point (2, -4) by reflection in X-axis is
3	The image of the point (2 , -1) by rotation about the origin point with an angle of measure 180° is
4	Translation $(x, y) \longrightarrow (x+1, y-3)$ maps the point $(3, 4)$ to
5	The image of the point $(2,3)$ by translation MN, in direction MN, where M $(2,-1)$, N $(5,1)$ is
6	The image of the point (2 5 – 4) by rotation about the origin point with an angle of measure 90° is
7	The image of the point by rotation about the origin point with an angle of measure 180° is $(-3, -2)$
8	The image of the point $(1, 3)$ by reflection in the X -axis is
9	The image of (3 > -4) by reflection in y-axis is
10	The image of the point (3, -2) by translation $(x, y) \longrightarrow (x-1, y+6)$ is
11	If $A = (x, y)$ is the image of A by the translation whose rule is $(x, y) = (x-3, y+1)$, then $A = \dots$
12	The image of the point (2,3) by rotation R (O,90°) is
13	The image of the point (4, -1) by rotation about the origin point with an angle of measure 180° is
14	The image of the point (2, 4) by reflection in y-axis is
15	The image of the point (2,5) by translation $(x,y) \longrightarrow (x+2,y-3)$ is

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16	If the image of the point $(-2, 4)$ by a translation is $(2, 5)$, then the image of the point $(2, -1)$ by the same translation is
17	The image of the point (2, -3) by rotation about the origin point with an angle measure 90° is
18	The image of the point (3 , - 8) by rotation about the origin point with an angles of measure 180° is
19	If \hat{A} (-3,-3) is the reflected image of the point $A(x,y)$ in the origin point (0,0), then $x = \dots$ and $y = \dots$
20	The image of the point (-1,3) by reflection in the y-axis is
21	The image of the point (-1,3) by translation (1,4) is
22	The image of the point (-5,6) by the translation (-2,3) is the point
23	The image of the point by rotation about the origin point with an angle of measure 90° is (-1,4)
24	The image of the point (3, 8) by rotation about the origin point with an angle of measure 180° is
25	If the image of the point A by reflection in the origin is \hat{A} (3, -2), then A is (
26	If the point \hat{A} (3, -2) is the image of A by reflection on the X-axis, then $A = (\dots, \dots)$
27	The image of the point $(2, 3)$ by translation $(4, -2)$ is
28	The image of the point $(5, -3)$ by translation 3 units in negative direction of X -axis is
29	The image of the point (-1,2) by rotation about the origin point with angle of measure 90° is
30	The image of (3,7) by rotation R (O, 180°) is

[C]: Essay Problems: -

In a cartesian plane draw the image of \triangle ABC where A (-2,3), B(2,3), C(2,6) 1 by translation $(x, y) \longrightarrow (x+2, y-1)$ 2018 Exam (9) Question (4) (b) Draw \triangle ABC in which AB = 3.5 cm. , m (\angle A) = 90° , AC=5 cm. 2 , then draw its image by reflection in AC 2017 Exam (9) Question (4)(a) Using the lattice, draw \triangle ABC where A (1,0), B (0,2) and C (-3,1) 3 , then draw its image by reflection in X-axis. 2017 Exam (1) Question (5) (b) Draw the triangle ABC in which: AB = AC = 5 cm, and BC = 6 cm., then draw 4 its image by rotation about A with an angle of mesure 180% 2016 Exam (13) Question (4) (b) Draw \triangle OBC on square lattice where: O(0,0), B(3,0) and C(0,4), then find its 5 image by rotation R (O > - 90°) 2016 Exam (10) Question (4) (a) Using the lattice, draw \triangle ABC in which A (-4,1), B (-1,3) and C (0,1) 6 , then draw the image of \triangle ABC by translation (2, 1) 2017 Exam (9) Question (3)(a) Draw the triangle ABC in which AB $\stackrel{1}{\sim} 3$ cm. $\stackrel{1}{\sim} BC = 4$ cm. $\stackrel{1}{\sim} AC = 5$ cm. 7 then draw its image by reflection in BC 2017 Exam (8) Question (5) (b) On a square lattice, draw \triangle ABC where A (1, 1), B (4, 1), C (4, 4) 8 then draw its image by reflection in X-axis. 2017 Exam (5) Question (3)(a) In the opposite figure : LMN is an equilateral triangle X, Y and Z are midpoints of LM MN and NL respectively." 9 Find: (1) The image of Δ LXZ by reflection in XZ (2) The image of \overline{XY} by rotation $(Y, 60^\circ)$ 2017 Exam (13) Question (3) (a) On a square lattice, draw \triangle ABC where: A (4,4), B (4,2) and C (1,2), then draw: (1) The image of \triangle ABC by reflection in the y-axis. 10 (2) The image of Δ ABC by rotation about the origin point with an angle of measure 270° 2016 Exam (11) Question (5) (a)

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11	Using the lattice, draw \overline{AB} where A (4,3), B (-1,1), then find the image of \overline{AB} by translation (X,Y) \longrightarrow (X+2,Y-1) 2018 Exam (14) Question (3) (b)
12	Draw the triangle ABC in which: AB = 7 cm., BC = 6 cm. and CA = 8 cm., then draw its image by reflection in BC 2016 Exam (10) Question (3) (b)
13	Draw Δ ABC where A (1,1), B (4,1), C (4,5) find its image by reflection in y-axis. By using square lattice. 2018 Exam (11) Question (4) (b)
14	In the opposite figure: ABCD is a square M is the intersection point of its diagonal find the image of Δ MAB by rotation about M with angle 90 C B 2018 Exam (7) Question (5) (a)
15	Draw Δ OBC on a square lattice where O (0,0), B(3,0), C (0,4), then draw its image by rotation about the origin point with an angle of measure 180° 2018 Exam (2) Question (5) (a)
16	On a square lattice, draw \triangle ABC where A (4,4), B (0,2), C (6,-2) then find its image by translation $(x,y) \longrightarrow (x-4,y+1)$
17	In the opposite figure: ABCD is a parallelogram, M is the point of intersection of its diagonals and $X \in AC$, $Y \in AC$, such that $C \in B$ Prove that: (1) \triangle ABX is the image of \triangle CDY by reflection in M (2) The figure XBYD is a parallelogram.
18	On a square lattice, draw the image of square ABDC where: A(1,2), B(-2,2), C(1,5), D(-2,5) by reflection in the y-axis. 2018 Exam (15) Question (4)(a)
19	On the square lattice draw \triangle ABC where A(1,1), B(4,1), C(4,4), then determine each of the following: (1) The image of \triangle ABC by reflex in y-axis. (2) The image of \triangle ABC by rotation about origin point with angle of measure 180°

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<u> </u>	
	If the image of the point A (1 1) has translation in the condition to the condition in A (2 2)
20	If the image of the point A (1, 1) by translation in the coordinate plane is A (2, 2)
	, find the images of the points O (0,0), B (4,2), C (-3,5) by the same translation. 2018 Exam (7) Question (4)(b)
	In the opposite figure:
	ABCD is a square, whose diagonals
21	intesect at M. Find the image of Δ MAB
	By rotation about M with angle of measure (-90°)
	В
	2018 Exam (14) Question (5) (b)
22	If the point A is the image of the point (-1,2) by reflection in y-axis, then find the
	image of A by translation (-1,2)
	Draw the image of the square ABCD where A(2,4), B(2,1), C(5,1), D(5,4)
23	by reflection in the χ -axis.
	In the opposite figure :
	ABCD is a square X, Y, Z, L are midpoints of AB, BC, CD and DA respectively.
	of \overline{AB} , \overline{BC} , \overline{CD} and \overline{DA} respectively
24	Find:
24	1) The image of Δ AML by translation with a magnitude $\frac{C}{V}$ B
	AM in direction AM
	② The image of ΔAML by rotation about the point M with an angle of measure – 90°
	(3) The image of \triangle AML by reflection in \overrightarrow{LY}
	2018 Exam (2) Question (4) (b)
25	Using the lattice, draw ABC where: A(2,3), B(4,2) and C(1,2)
25	then draw its image by rotation about the origin point with an angle of measure 180°
	In the opposite figure: 2016 Exam (15) Question (3) (a) X 9cm. L
	XYZL is a trapezium, in which
	$\overline{XL} // \overline{YZ}$, $m(\angle Y) = 90^{\circ}$
26	$,\overline{LM}\perp\overline{YZ},YZ=ZL=17 \text{ cm.},XL=9 \text{ cm.}$
	Find: The length of \overline{XY} Y M Z 17cm.
	The image of \overline{XL} by translation of magnitude XY in the direction of \overline{XY}
	2018 Exam (3) Question (5)
1	

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27	In a Cartesian plane draw the image of \triangle ABC Where A (1,0), B (0,2), C (-3,1) by translation $(X,y) \longrightarrow (X+2,y-1)$ 2017 Exam (8) Question (4) (b)
28	On a square lattice, draw \triangle ABC where: A (4,4), B (4,2) and C (1,2), then find its image by reflection in the y-axis.
29	In the opposite figure: ABCDEF is a regular hexagon Find the image of \triangle ABM by: ① Reflection on EB ② Translation FE in direction of FE ③ Rotation (M, 120°) ④ Reflection in M ⑤ Rotation (M, 300°)
30	Using the square lattice: Draw \triangle XYZ in which X (4,1), Y (5,0), Z ($\frac{1}{2}$ 1,-2), then draw its image by rotation about the origin point with an angle of measure (-180°) 2018 Exam (13) Question (3) (a)
31	Complete: Rotation in a plane reserve ,
32	On the square lattice, draw \triangle ABC in which $A(-2,2)$, $B(1,4)$ and $C(3,1)$, then find the image of \triangle ABC by translation $(2,1)$
33	Draw the triangle ABC in which AB = 3 cm. , BC = 4 cm. , m (\angle B) = 90°, then draw its image by reflection in straight line BC
34	In a square lattice, draw the triangle OBC in which O (0,0), B (3,0), C (1,2) then find its image by reflection in the y-axis. 2017 Exam (14) Question (5) (a)
35	A rectangle its vertices are $A(-1,-2)$, $B(7,2)$, $C(5,6)$ and $D(-3,2)$ Find the image of the vertices by rotation around the origin point with an angle of measure 180°
	2017 Exam (4) Question (5) (a)

ألتب ذاكرولي في البحث وانض لجروبات ذاكرولي من رياض الاطفال للصف الثالث الاعدادي